KING EDWARD VI
HANDSWORTH GRAMMAR
SCHOOL FOR BOYS

KING EDWARD VI
ACADEMY TRUST
BIRMINGHAM

Year 10

2026 Mathematics 2027

Unit 17 Student – Part 1

HGS Maths

Tasks

Dr Frost Course

Name: _____

Class: _____

KING EDWARD VI
HANDSWORTH GRAMMAR
SCHOOL FOR BOYS

KING EDWARD VI
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Year 10

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Unit 17 Student – Part 2

HGS Maths

Tasks

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Name: _____

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2 Basic Circle Theorems
3 Direct and Inverse Proportion
4 Constructions and Loci

1 Bounds and Error Intervals

Worked Example	Your Turn
A number z, when rounded to the nearest 100, is equal to 6700. Find the upper and lower bound of z.	A number z, when rounded to the nearest 10, is equal to 740. Find the upper and lower bound of z.

Worked Example	Your Turn
A number x, when rounded to 3 decimal places, is equal to 0.007. Find the upper and lower bound of x.	A number x, when rounded to 2 decimal places, is equal to 0.03. Find the upper and lower bound of x.

Worked Example	Your Turn
A number x, when rounded to 3 significant figures, is equal to 612000. Find the upper and lower bound of x.	A number x, when rounded to 2 significant figures, is equal to 35000. Find the upper and lower bound of x.

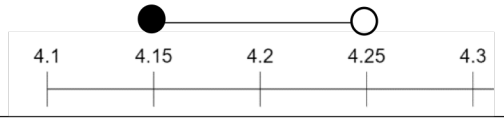
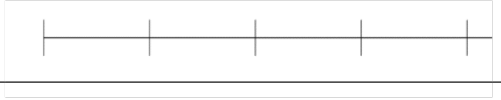
Worked Example	Your Turn
A number y, when rounded to 1 decimal place, is equal to 8.2. Find the error interval for y.	A number y, when rounded to the nearest 10, is equal to 680. Find the error interval for y.

Fill in the Gaps

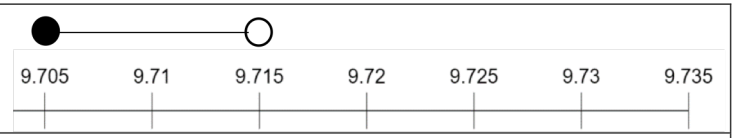
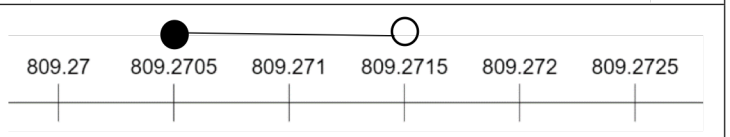
x	Level of Accuracy	Lower Bound	Upper Bound	Error Interval
30	*to the nearest* 10	25		$25 \leq x < 35$
700	*to the nearest* 100		750	
25	*to the nearest integer*		25.5	
25	*to the nearest* 5	22.5		
24000	*to the nearest* 1000			
7.8	*to the nearest* 0.1			
360	*to the nearest* 20			
360	*to the nearest integer*			
6000	*to the nearest* 100			
200	*to the nearest* 5			
200	*to the nearest* 10			
13	*to the nearest tenth*			
	to the nearest integer		8.5	
		49500	50500	
8				$7 \leq x <$

x	Level of Accuracy	Lower Bound	Upper Bound	Error Interval
6.4	*to* 1 *decimal place*	6.35		$6.35 \leq x < 6.45$
7	*to the nearest integer*		7.5	
7.3	*to* 1 *decimal place*	7.25		
5.19	*to* 2 *decimal places*			
12.3	*to the nearest* 0.1			
40	*to* 1 *significant figure*		45	
1.5	*to* 2 *significant figures*			
0.76	*to* 2 *decimal places*			
10	*to* 1 *significant figure*			
27	*to the nearest integer*			
27.9	*to* 1 *decimal place*			
654	*to* 3 *significant figures*			
	to 1 *significant figure*	75		
		5.35	5.45	
				$95 \leq x < 150$

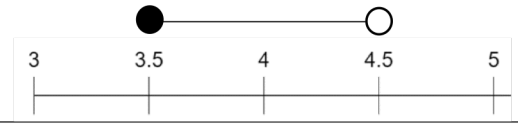
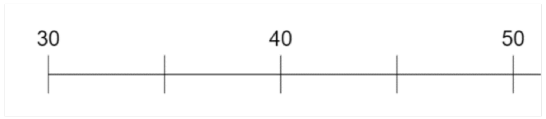
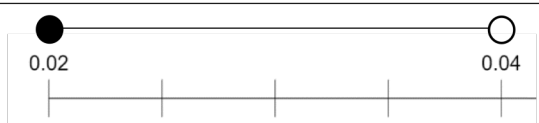
Fill in the Gaps

Value	Rounded to	Lower Bound	Upper Bound	Error Interval	Inequality on a number line
4.2	1 dp	4.15	4.25	$4.15 \leq x < 4.25$	
3.2	1 dp			$\leq x <$	
3.6	1 dp			$\leq x <$	
3.68	2 dp	3.675	3.685	$\leq x <$	
8.63	2 dp			$\leq x <$	
8.43	2 dp				
	2 dp	8.815	8.825		
	2 dp	9.615	9.625		

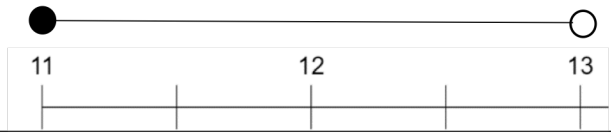
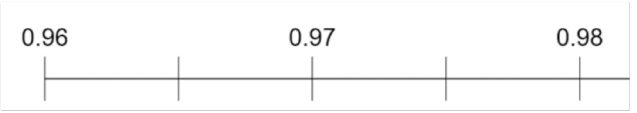
Fill in the Gaps

					
				$9.685 \leq x < 9.695$	
9.685	3 dp	9.6845	9.6855		
90.685	3 dp				
58.690	3 dp				
	3 dp				
	3 dp			$\leq x < 812.3275$	
	3 dp			$42.3795 \leq x <$	

Fill in the Gaps

Value	Rounded to	Lower Bound	Upper Bound	Error Interval	Inequality on a number line
4	$1\ sf$	3.5	4.5	$3.5 \leq x < 4.5$	
40	$1\ sf$	35		$\leq x <$	
30	$1\ sf$			$\leq x <$	
200	$1\ sf$			$\leq x <$	
0.7	$1\ sf$		0.75	$\leq x <$	
0.08	$1\ sf$				
	$1\ sf$			$8.5 \leq x < 9.5$	
	$1\ sf$				

Fill in the Gaps

12	2 sf	11.5	12.5	$11.5 \leq x < 12.5$	
0.97	2 sf				
760	2 sf				
7.68	3 sf				
9.61	3 sf				
					
	1 sf			$\leq x < 7.5$	
	2 sf			$435 \leq x <$	

Fill in the Gaps

Number	Rounding	Lower bound	Upper bound	Error interval
4	Nearest integer	3.5	4.5	
40	Nearest ten			$35 \leq x < 45$
40	Nearest integer	39.5	40.5	
50	Nearest integer	49.5		
50	Nearest ten		55	
550		545		
5.5	1 decimal place			
55.5	1 decimal place			
89.6	1 decimal place			
50	1 significant figure			

Fill in the Gaps

measurement	precision	inequality	lower bound	upper bound
48.3	1 dp			
	..... sf	$38.5 \leq x < 39.5$		
230	nearest 10			
	nearest 7	$52.5 \leq x <$.....		
23.10	4 sf			
	..... dp		23.2285	23.2295
1000	nearest whole number			
1000	nearest 10			
1000	3 sf			
1000	2 sf			
	..... sf	$950 \leq x < 1500$		
	1 sf		0.00035	

Worked Example	Your Turn
The number of people on a bus is given as 50, correct to the nearest 10. What is the lowest and highest possible number of people on the bus?	There are 9500 red pandas left in the wild. This number is accurate to the nearest 500. What are the smallest and largest number of red panda that can be left?

Worked Example	Your Turn
$p = 5qr$ $q = 0.709$ correct to 3 significant figures. $r = 0.071$ correct to 3 decimal places. Work out the lower bound for the value of p Give your answer correct to 3 decimal places when appropriate.	$a = 5bc$ $b = 0.124$ correct to 3 decimal places. $c = 98000$ correct to 2 significant figures. Work out the lower bound for the value of a Give your answer correct to 3 decimal places when appropriate.

Worked Example	Your Turn
$p = 4q + 2r$ $q = 907000$ correct to 3 significant figures. $r = 8.88$ correct to 2 decimal places. Work out the lower bound for the value of p Give your answer correct to 3 decimal places when appropriate.	$a = 4b + 3c$ $b = 55.4$ correct to 1 decimal place. $c = 3.1$ correct to 2 significant figures. Work out the lower bound for the value of a Give your answer correct to 3 decimal places when appropriate.

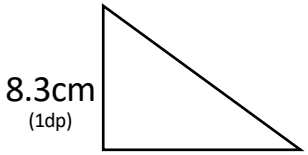
Worked Example	Your Turn
$p = 5q - 5r$ $q = 0.003$ correct to 1 significant figure. $r = 1.93$ correct to 2 decimal places. Work out the lower bound for the value of p Give your answer correct to 3 decimal places when appropriate.	$a = 3b - 2c$ $b = 98.9$ correct to 1 decimal place. $c = 26.5$ correct to 3 significant figures. Work out the upper bound for the value of a Give your answer correct to 5 decimal places when appropriate.

Worked Example	Your Turn
$p = \frac{2q}{r}$ $q = 0.9$ correct to 1 significant figure. $r = 0.075$ correct to 3 decimal places. Work out the lower bound for the value of p Give your answer correct to 3 decimal places when appropriate.	$a = \frac{4b}{c}$ $b = 78.4$ correct to 1 decimal place. $c = 4150$ correct to 3 significant figures. Work out the lower bound for the value of a Give your answer correct to 3 decimal places when appropriate.

Worked Example	Your Turn
$p = \frac{q}{r-s}$ $q = 5$ correct to 1 significant figure. $r = 0.002$ correct to 1 significant figure. $s = 0.645$ correct to 3 decimal places. Work out the lower bound for the value of p Give your answer correct to 3 decimal places when appropriate.	$x = \frac{y}{z-w}$ $y = 0.786$ correct to 3 decimal places. $z = 702$ correct to 3 significant figures. $w = 0.5$ correct to 1 significant figure. Work out the lower bound for the value of x Give your answer correct to 5 decimal places when appropriate.

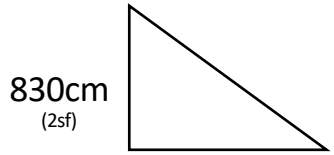
Worked Example

The height and width of the triangle below have been rounded as shown in brackets.
Work out the LB and UB for the **area** of the triangle.



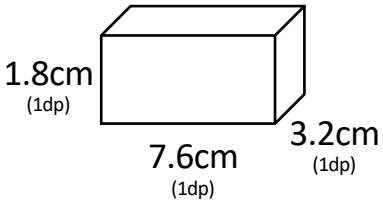
Your Turn

The height and width of the triangle below have been rounded as shown in brackets.
Work out the LB and UB for the **area** of the triangle.



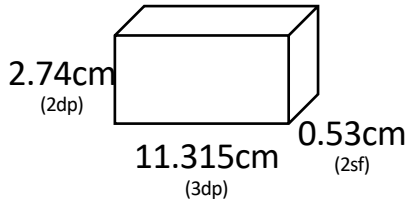
Worked Example

The dimensions of the cuboid below have been rounded as shown in brackets.
Work out the LB and UB for the **volume** of the cuboid.



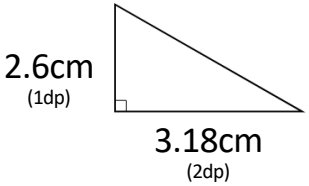
Your Turn

The dimensions of the cuboid below have been rounded as shown in brackets.
Work out the LB and UB for the **volume** of the cuboid.



Worked Example

Use Pythagoras' Theorem to find the LB and UB of the missing sides below.
All lengths have been rounded as shown in brackets.



Your Turn

Use Pythagoras' Theorem to find the LB and UB of the missing sides below.
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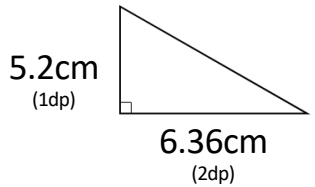

Worked Example

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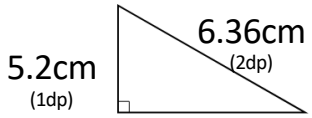
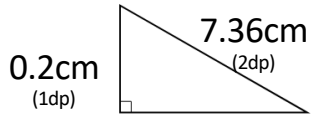


Your Turn

Use Pythagoras' Theorem to find the LB and UB of the missing sides below.
All lengths have been rounded as shown in brackets.



Fill in the Gaps

a. b and c are all rounded to the degree of accuracy stated. Find the maximum and minimum values for x.
Values given for $x_{\max}$ are exact.

a	b	c	Equation	$x_{\max}$	$x_{\min}$
10 (1 sig fig)	12.1 (3 sig fig)	3.4 (2 sig fig)	$\sqrt{ax} = b - c$		
0.5 (1 sig fig)	4.5 (2 sig fig)	−2.0 (2 sig fig)	$\frac{a}{x} = b^2 + 3c$		
5.2 (2 sig fig)	3.4 (2 sig fig)	5 (1 sig fig)	$\frac{ax^2}{b} = c$		
3 (1 sig fig)	4 (1 sig fig)	8 (1 sig fig)	$ax + c = b$		
5 (1 sig fig)	−3 (1 sig fig)	☐ (2 sig fig)	$ax = bc$	−3.25	
☐ (2 sig fig)	4.3 (2 sig fig)	0.3 (1 sig fig)	$a + x = \frac{b}{c}$	9.35	

Considering Bounds

Worked Example	Your Turn
$a = \frac{\sqrt{b}}{c}$ $b = 0.24$ correct to 2 decimal places. $c = 57.2$ correct to 3 significant figures. By considering bounds, work out the value of a, giving your answer to a suitable degree of accuracy.	$a = \frac{b}{\sqrt{c}}$ $b = 0.359$ correct to 3 significant figures. $c = 0.64$ correct 2 decimal places. By considering bounds, work out the value of a, giving your answer to a suitable degree of accuracy.

Truncation

Worked Example	Your Turn
Truncate 41.53681 to: a) 1 decimal place b) 2 decimal places c) 3 decimal places	Truncate 11.95291 to: a) 1 decimal place b) 2 decimal places c) 3 decimal places

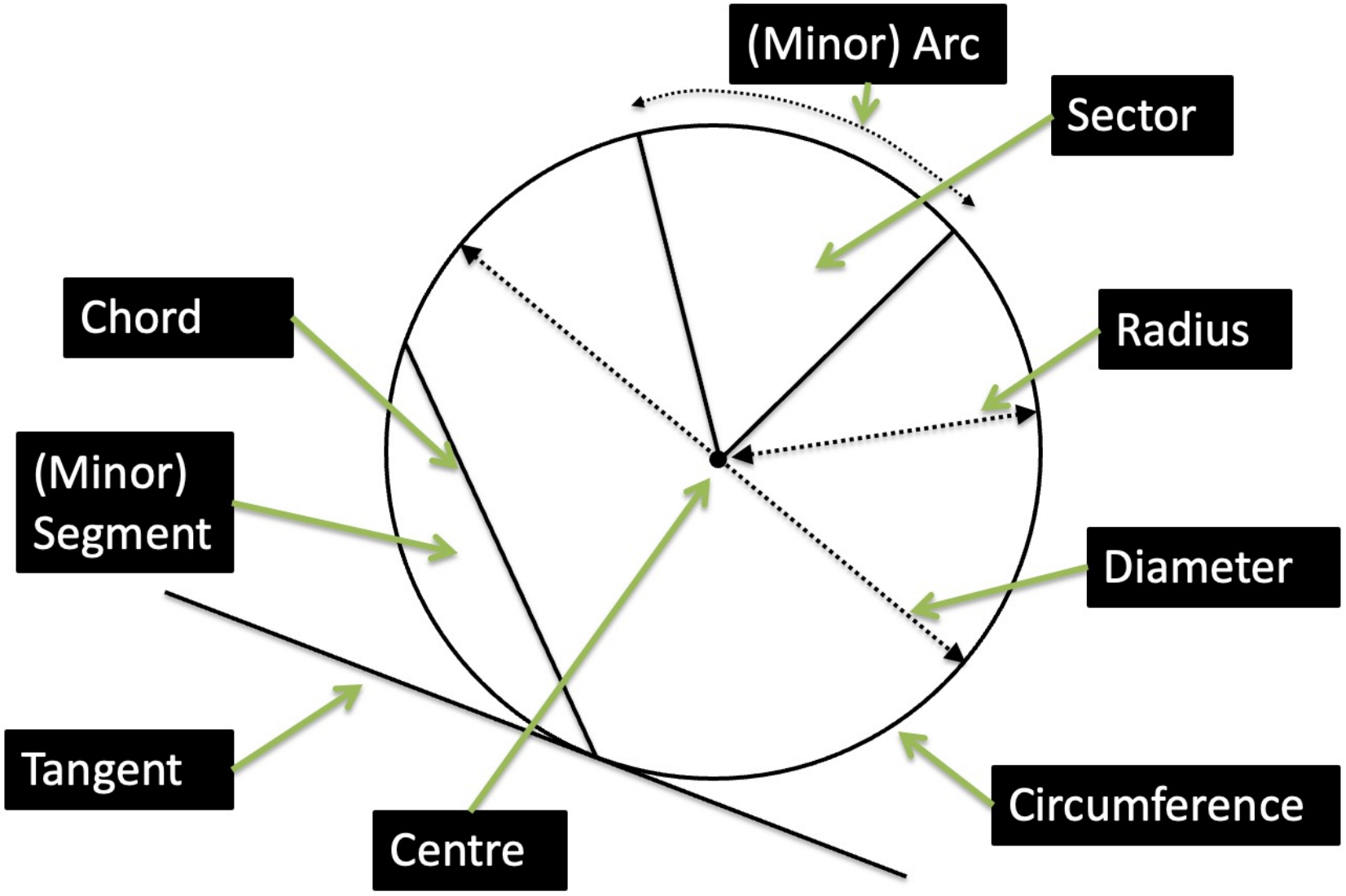
Worked Example	Your Turn
A number z, when truncated to 2 decimal places, is equal to 4.97. Find the upper and lower bound of z.	A number x, when truncated to 3 decimal places, is equal to 0.545. Find the upper and lower bound of x.

Dr Frost 383b and 310d

Extra Notes

2 Basic Circle Theorems

Parts of a Circle



Fluency Practice

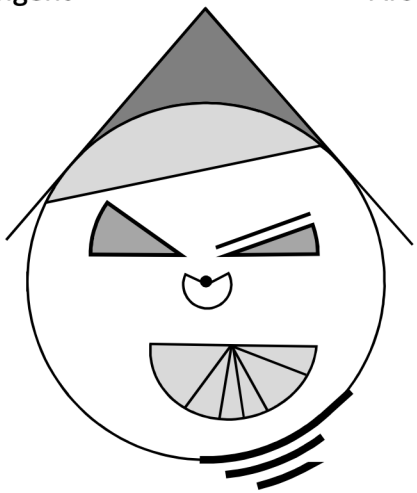
Circle Vocabulary: Match each word with its definition.

Arc	Line joining two points on a circumference.
Segment	Perimeter of a circle.
Chord	Part of a circle between a chord and an arc.
Radius	Line touching the circumference of a circle once.
Diameter	Distance from the centre of a circle to the edge.
Circumference	Part of the circumference of a circle.
Tangent	Part of a circle between two radii and an arc.
Sector	Width of a circle.

Circle Vocabulary: Label the diagram using parts of a circle.

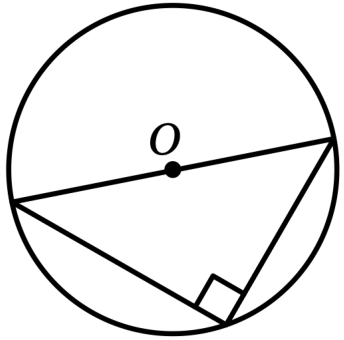
Circumference Diameter Chord Radius Sector

Centre Tangent Arc Segment

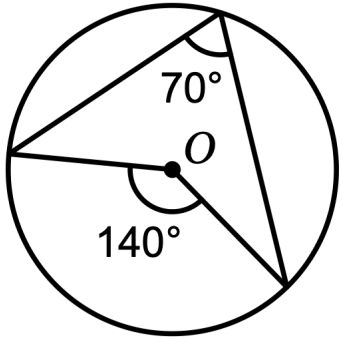


Circle Theorems 1

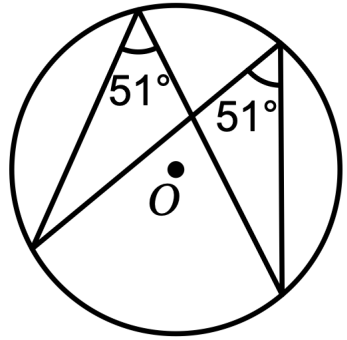
The angle in a semicircle is a right angle.



The angle at the centre is twice the angle at the circumference.

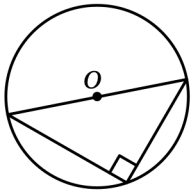
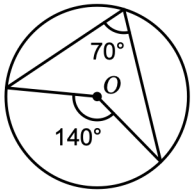
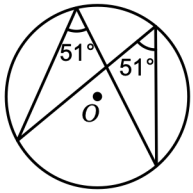


Angles in the same segment are equal.



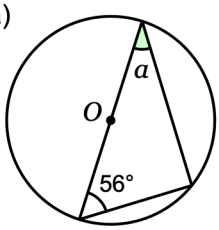
Dr Frost 442c, 442a and 442b

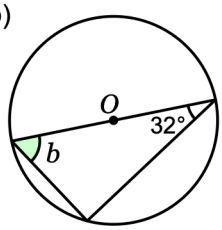
rules

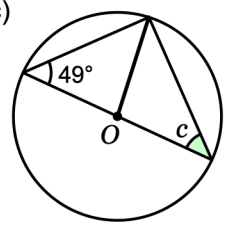
The angle in a semicircle is a right angle.	The angle at the centre is twice the angle at the circumference.	Angles in the same segment are equal.
		

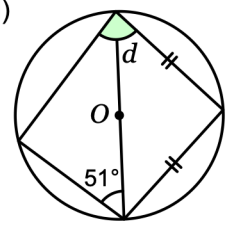
exercise

1. Work out the angles marked with letters.

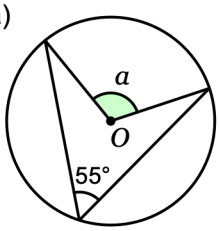
a) 

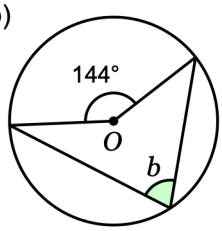
b) 

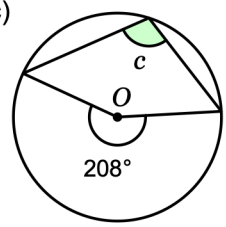
c) 

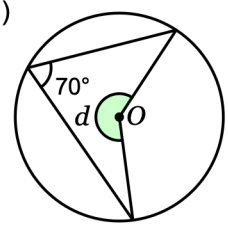
d) 

2. Work out the angles marked with letters.

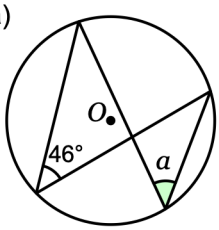
a) 

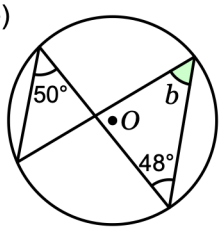
b) 

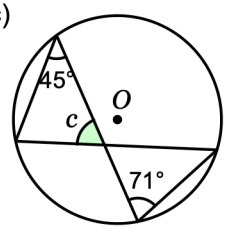
c) 

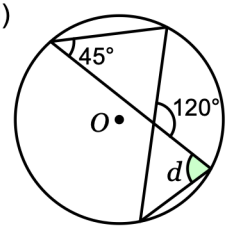
d) 

3. Work out the angles marked with letters.

a) 

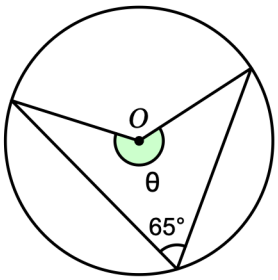
b) 

c) 

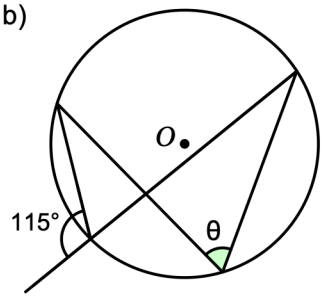
d) 

4. Work out the angles marked θ.

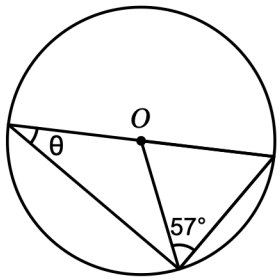
a)



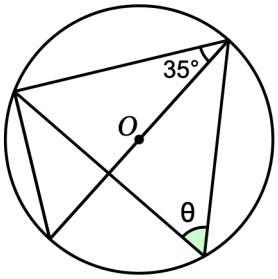
b)



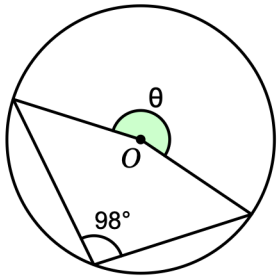
c)



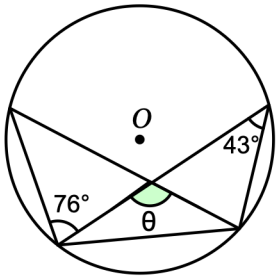
d)



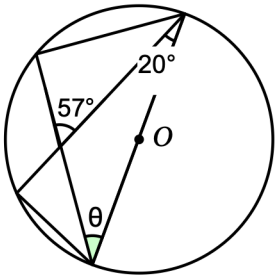
e)



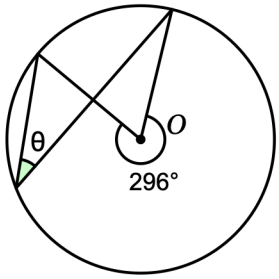
f)



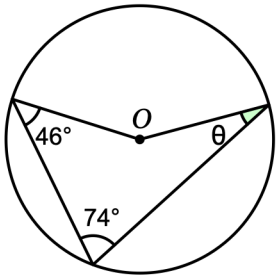
g)



h)

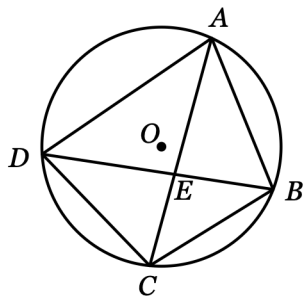


i)



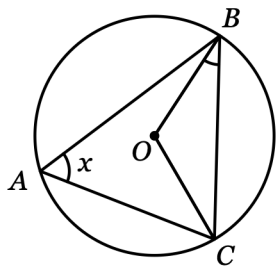
5. Points A, B, C and D lie on the circumference of a circle.
AEC and DEB are straight lines.

Prove that triangles ABE and DCE are similar.



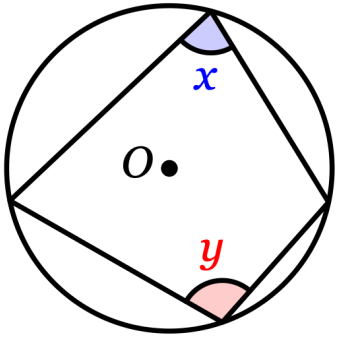
6. A, B and C are points on a circle with centre O.
$\angle BAC = x$

Show that: $\angle OBC = 90 - x$



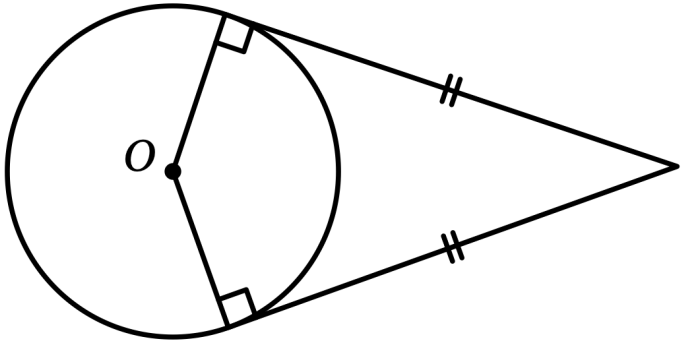
Circle Theorems 2

Opposite angles of a cyclic quadrilateral sum to 180°.



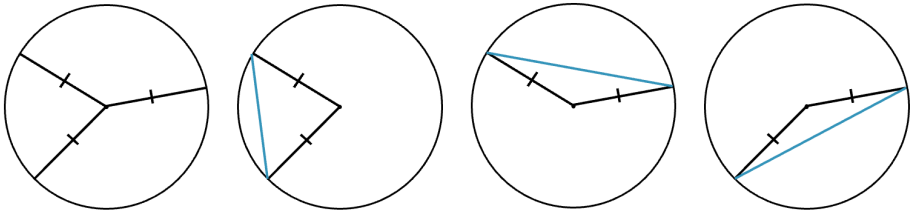
$x + y = 180°$

Tangents to a point are equal in length.



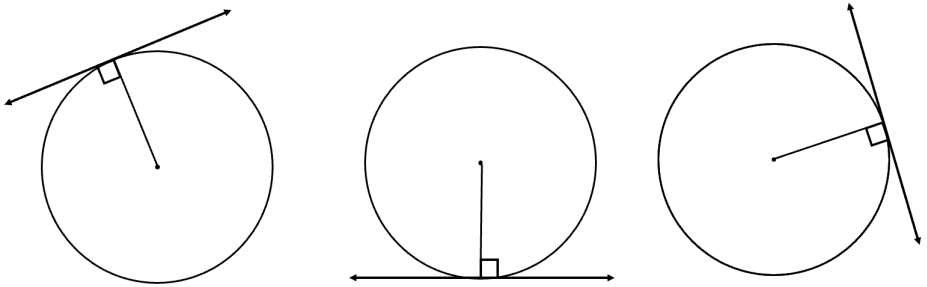
A radius is always the same length, wherever we draw it.

When we draw two radii, we can make an isosceles triangle.



If we draw a tangent, we can draw a radius to meet it.

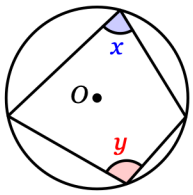
When a tangent meets a radius, they are perpendicular.



Dr Frost 442d, 442g and 442e

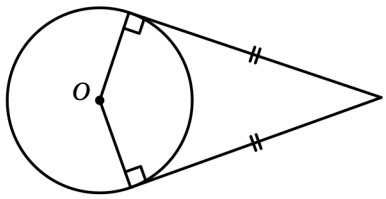
rules

Opposite angles of a cyclic quadrilateral sum to 180°.



$x + y = 180°$

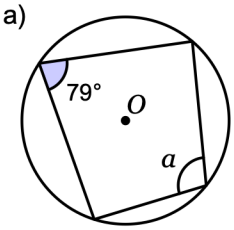
Tangents to a point are equal in length.



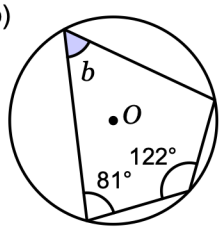
exercise

1. Work out the angles marked with letters.

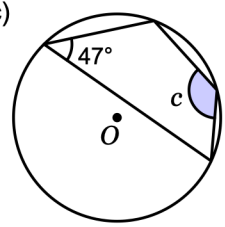
a)



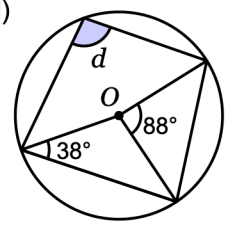
b)



c)

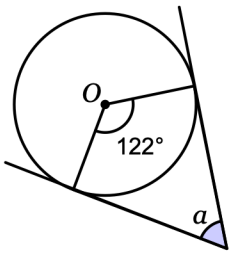


d)



2. Work out the angles marked with letters.

a)



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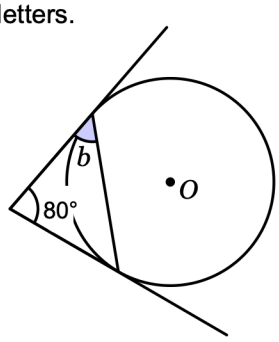
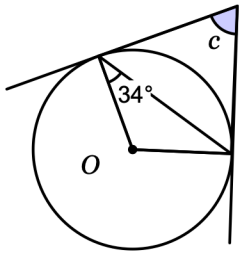
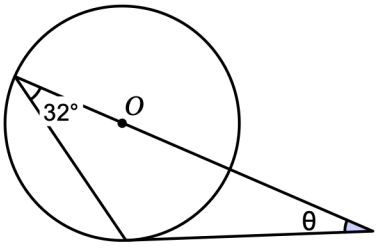


c)



3. Work out the angles marked θ.

a)



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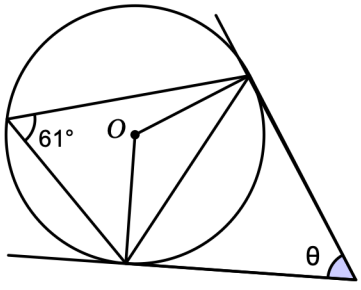
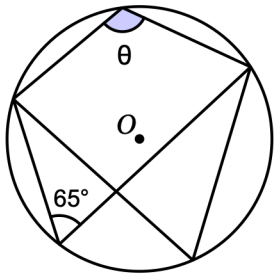
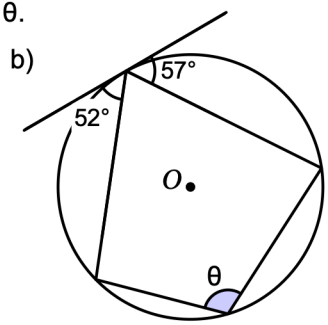


4. Work out the angles marked θ.

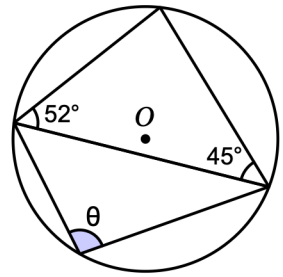
a)



b)



c)



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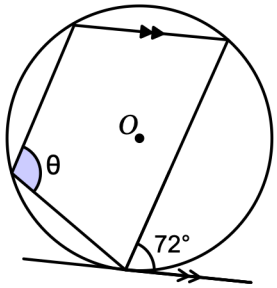
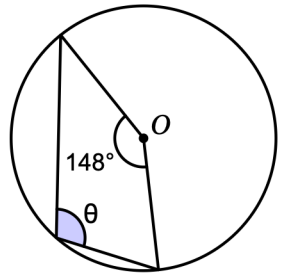


e)



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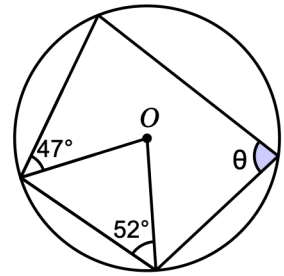
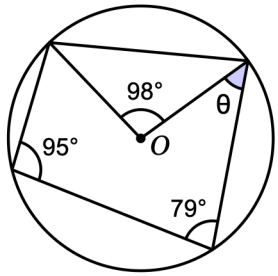
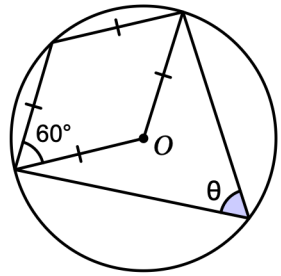


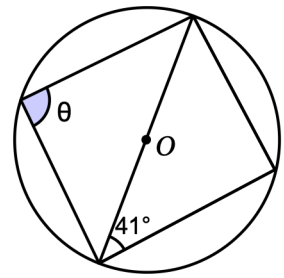
g)



h)

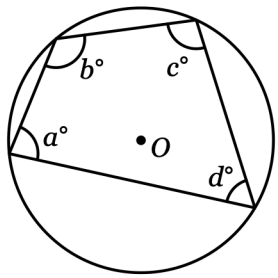


i)



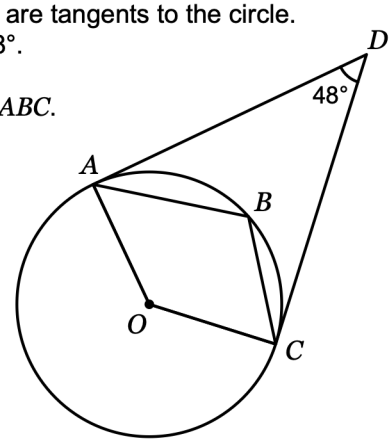
5. $a : b : c = 4 : 6 : 5$.

Work out the values of a, b, c and d.



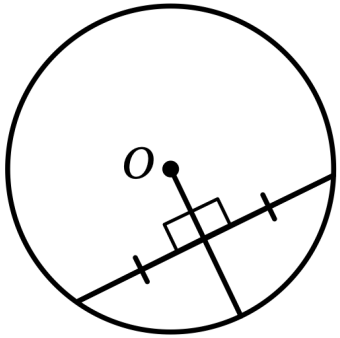
6. A, B and C are points on the circumference of a circle with centre O.
AD and CD are tangents to the circle.
$\angle ADC = 48°$.

Work out $\angle ABC$.

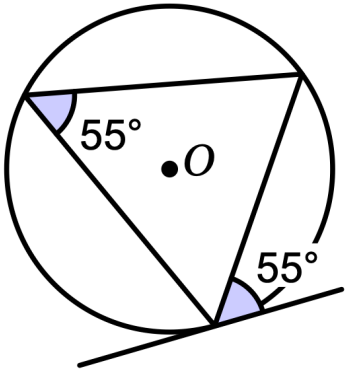


Circle Theorems 3

The perpendicular from the centre to a chord bisects the chord.

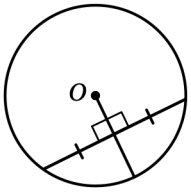


The angle between a chord and a tangent equals the angle in the **alternate segment**.

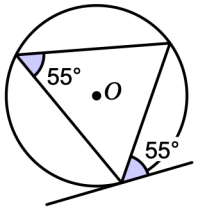


rules

The perpendicular from the centre to a chord bisects the chord.



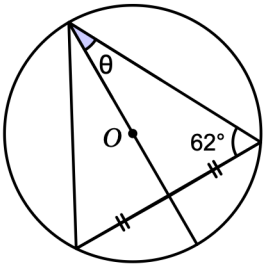
The angle between a chord and a tangent equals the angle in the **alternate segment**.



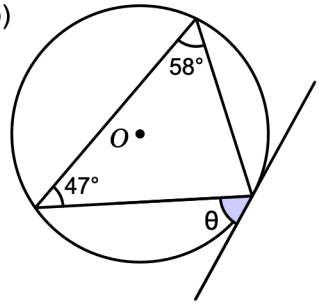
exercise

1. Work out the angles marked θ.

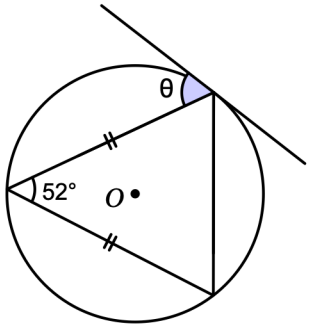
a)



b)



c)



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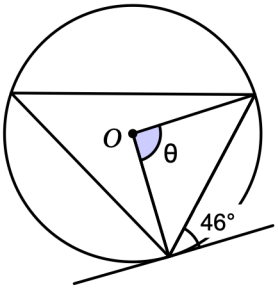
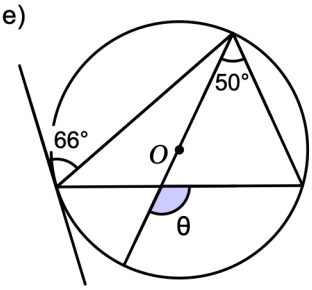


e)



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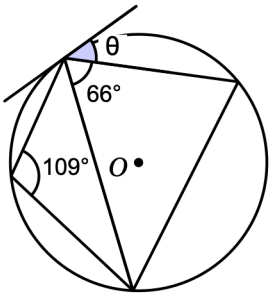

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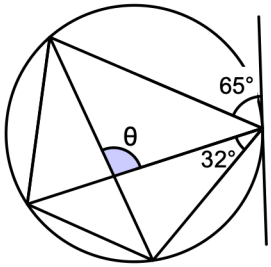

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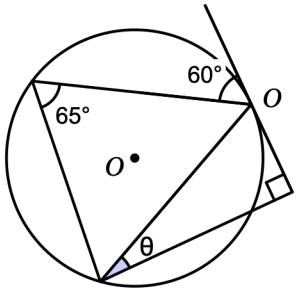

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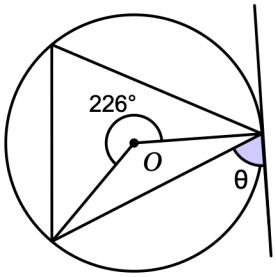
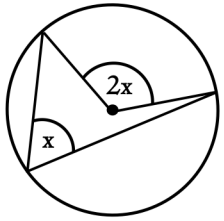
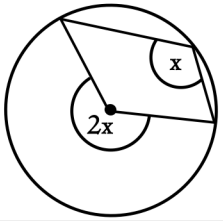
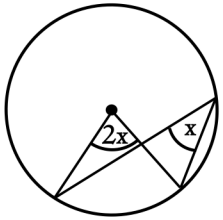


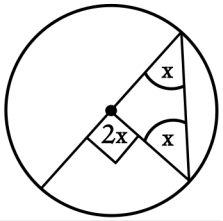
Circle Theorems Summary

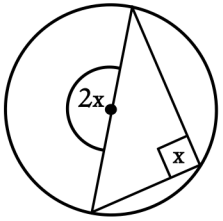
What you need to remember when answering Circle Theorems questions





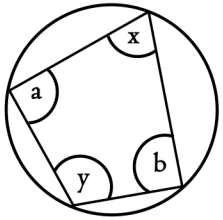




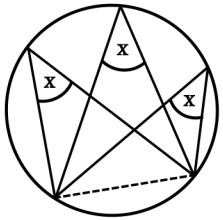


The angle at the centre of a circle is twice the angle at the circumference, so…

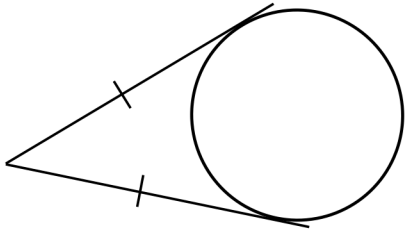
…the angle in a semi-circle is 90°



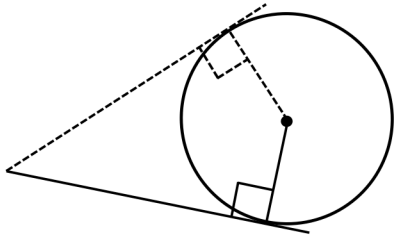
Opposite angles in a cyclic quadrilateral add up to 180°



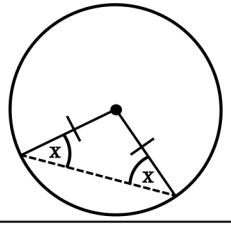
Angles subtended by the same arc [or chord] are equal in size



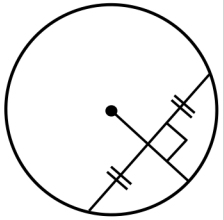
Tangents from the same point are equal in length



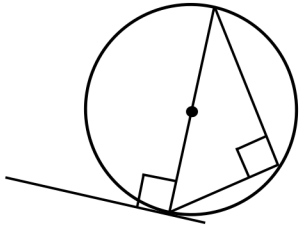
A radius and a tangent form a right angle

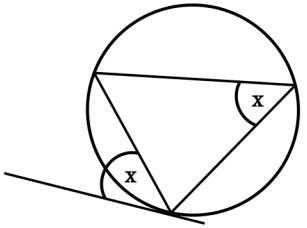


Two radii make an isosceles triangle

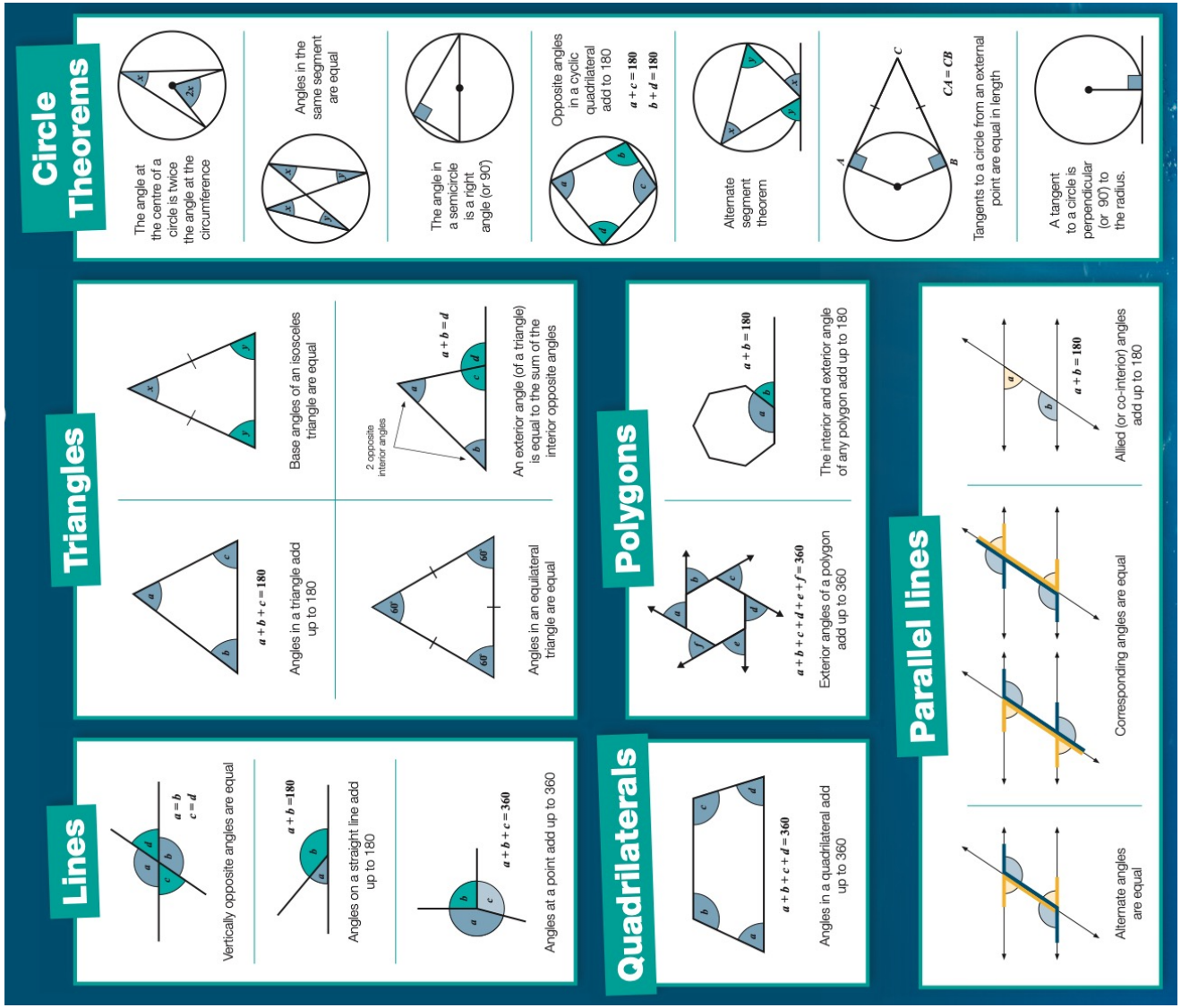


The perpendicular bisector of a chord passes through the centre of the circle



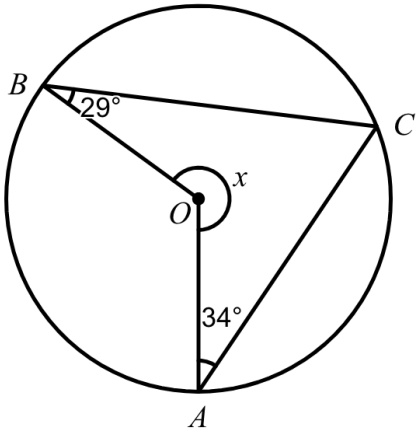


The angle between a tangent and a chord [or diameter] is equal to the angle in the alternate segment


Lines
a = b
c = d
Vertically opposite angles are equal
a + b = 180
Angles on a straight line add up to 180
a + b + c = 360
Angles at a point add up to 360
Triangles
a + b + c = 180
Angles in a triangle add up to 180
Base angles of an isosceles triangle are equal
2 opposite interior angles
a + b = d
An exterior angle (of a triangle) is equal to the sum of the interior opposite angles
60°
60°
60°
Angles in an equilateral triangle are equal
Quadrilaterals
a + b + c + d = 360
Angles in a quadrilateral add up to 360
Polygons
a + b = 180
a + b + c + d + e + f = 360
Exterior angles of a polygon add up to 360
The interior and exterior angle of any polygon add up to 180
Parallel lines
Alternate angles are equal
Corresponding angles are equal
a + b = 180
Allied (or co-interior) angles add up to 180
Circle Theorems
The angle at the centre of a circle is twice the angle at the circumference
Angles in the same segment are equal
The angle in a semicircle is a right angle (or 90°)
Opposite angles in a cyclic quadrilateral add to 180
a + c = 180
b + d = 180
Alternate segment theorem
CA = CB
Tangents to a circle from an external point are equal in length
A tangent to a circle is perpendicular (or 90°) to the radius.

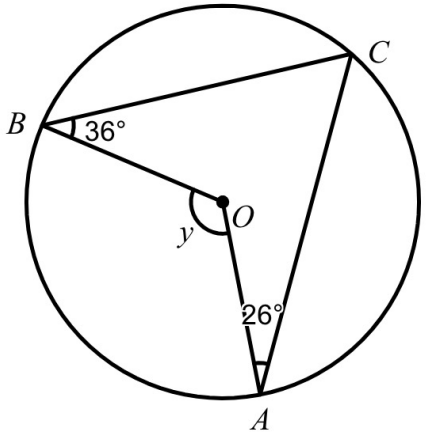
Worked Example

Find the value of x



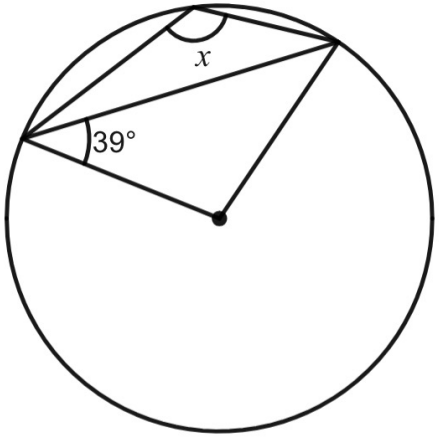
Your Turn

Find the value of y



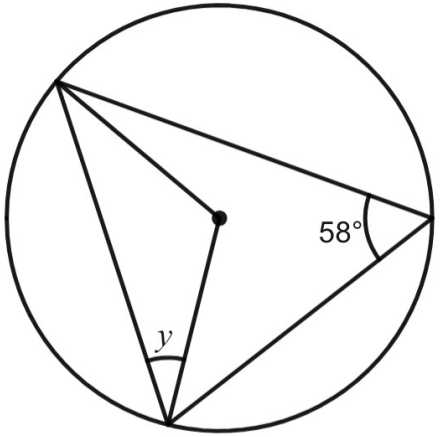
Worked Example

Find the value of x



Your Turn

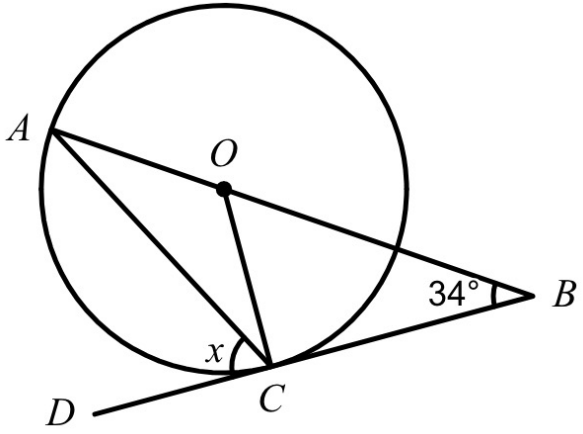
Find the value of y



Worked Example

AOB is a straight line.
DCB is the tangent to the circle at C

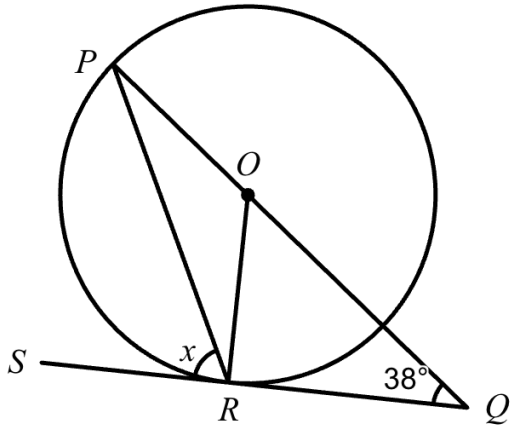
Find the value of x



Your Turn

POQ is a straight line.
SRQ is the tangent to the circle at R

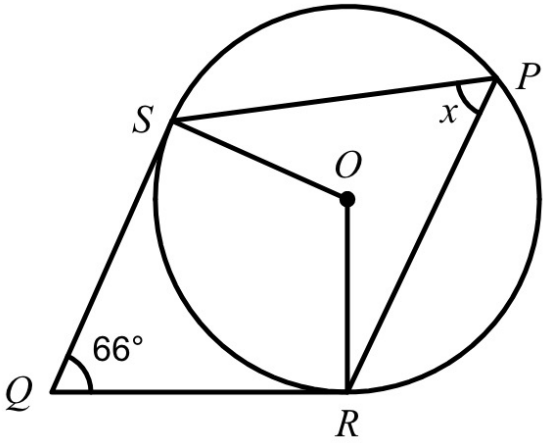
Find the value of y



Worked Example

RQ and QS are tangents to the circle at R and S

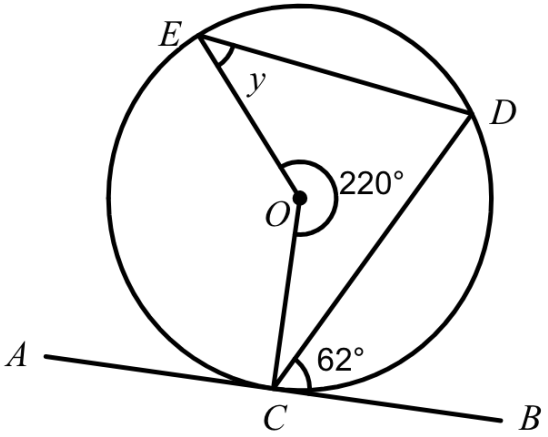
Find the value of x



Your Turn

ACB is the tangent to the circle at C

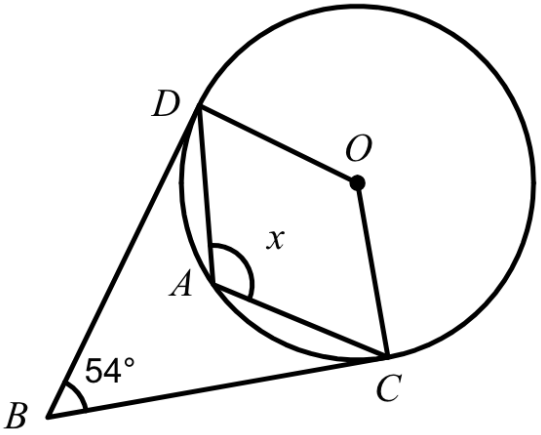
Find the value of y



Worked Example

CB and BD are tangents to the circle at C and D

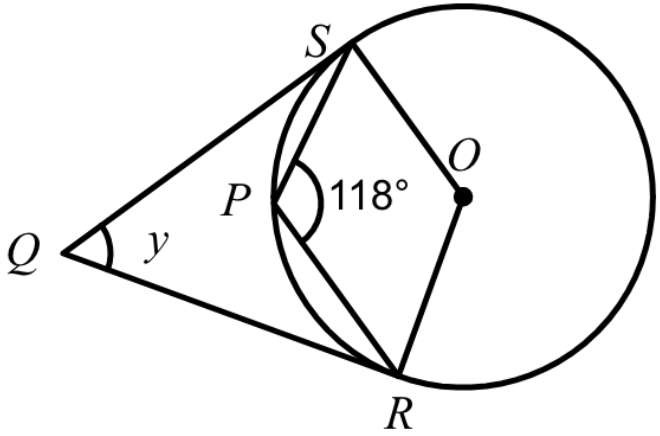
Find the value of x



Your Turn

RQ and QS are tangents to the circle at R and S

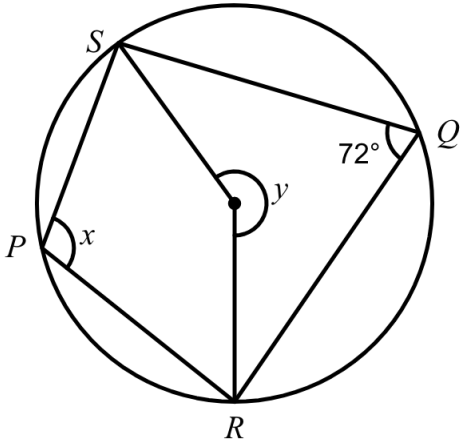
Find the value of y



Dr Frost 442m

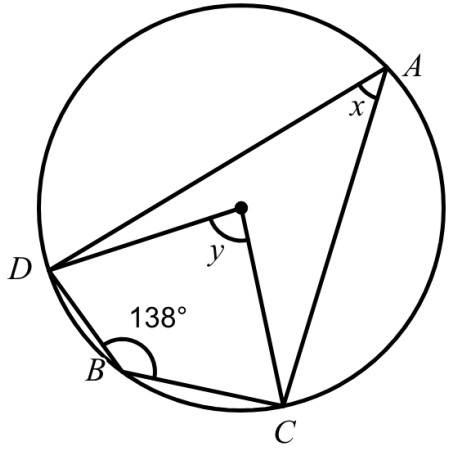
Worked Example

Find the values of x and y



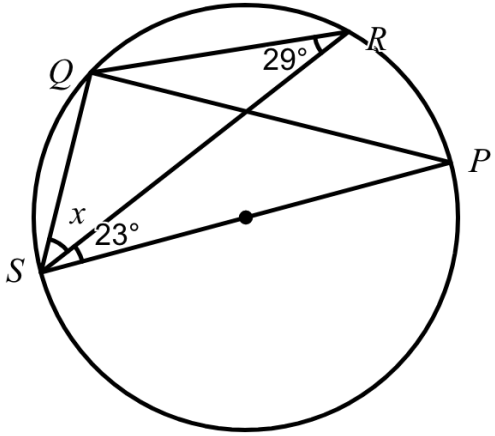
Your Turn

Find the values of x and y



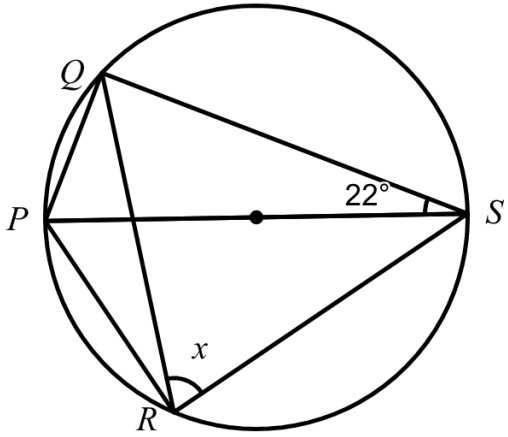
Worked Example

Find the value of x



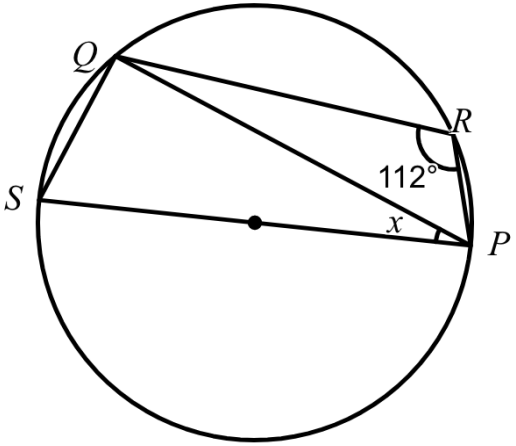
Your Turn

Find the value of x



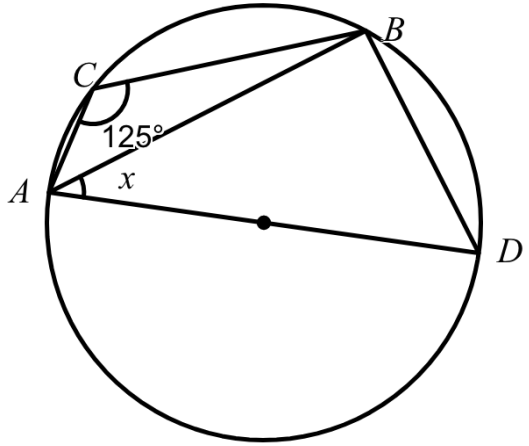
Worked Example

Find the value of x



Your Turn

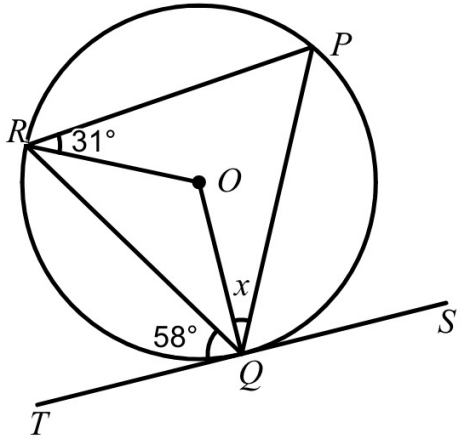
Find the value of x



Worked Example

ST is a tangent to the circle at Q

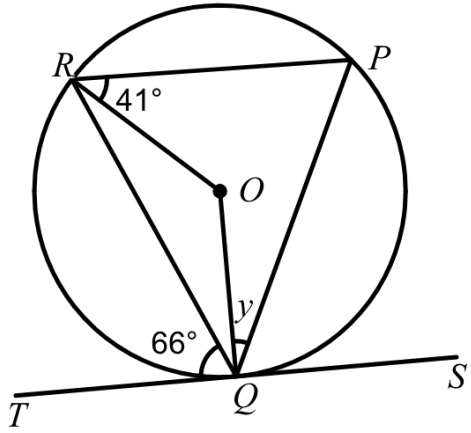
Find the value of x



Your Turn

ST is a tangent to the circle at Q

Find the value of y

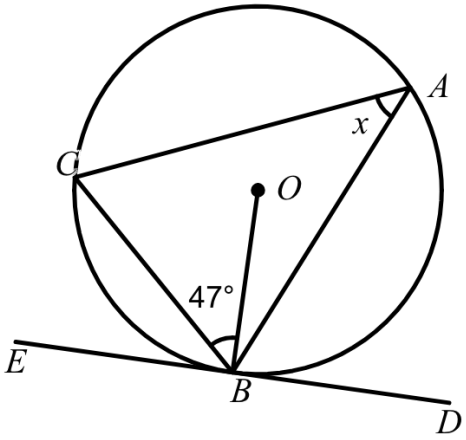


Dr Frost 442q

Worked Example

DE is a tangent to the circle at B

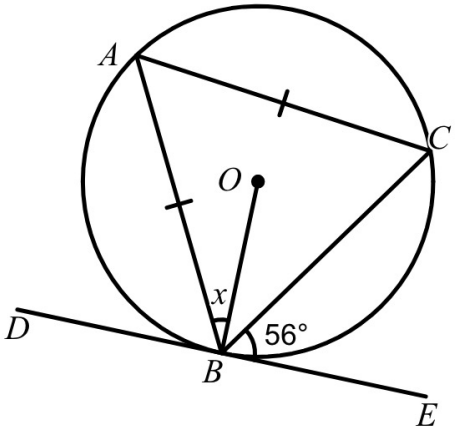
Find the value of x



Your Turn

DE is a tangent to the circle at B
$AB = AC$

Find the value of x

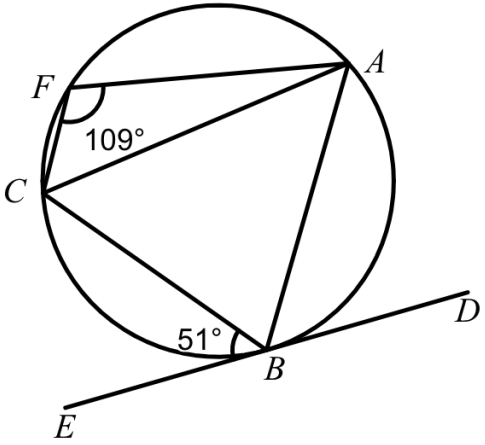


Dr Frost 442r

Worked Example

DE is a tangent to the circle at B

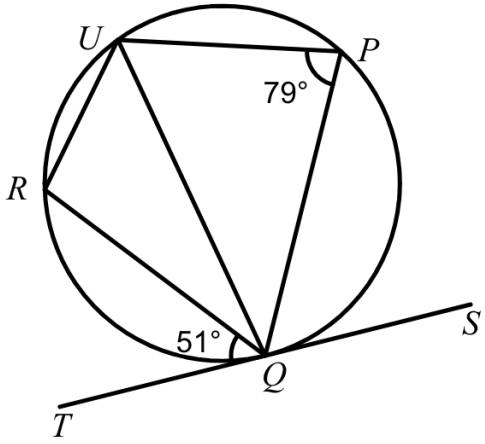
Find the value of $\angle BCA$



Your Turn

ST is a tangent to the circle at Q

Find the value of $\angle RQU$

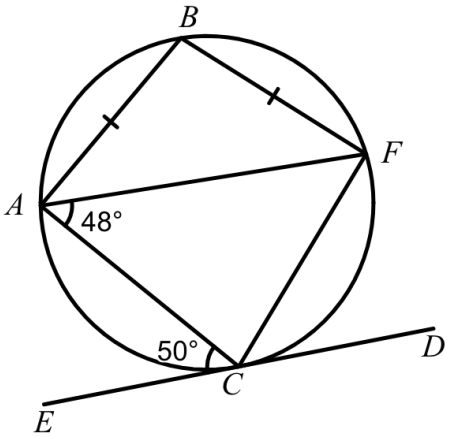


Dr Frost 442s

Worked Example

DE is a tangent to the circle at B

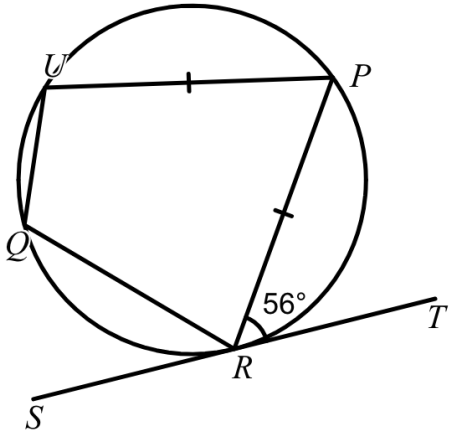
Find the value of $\angle FAB$



Your Turn

ST is a tangent to the circle at Q

Find the value of $\angle RQU$

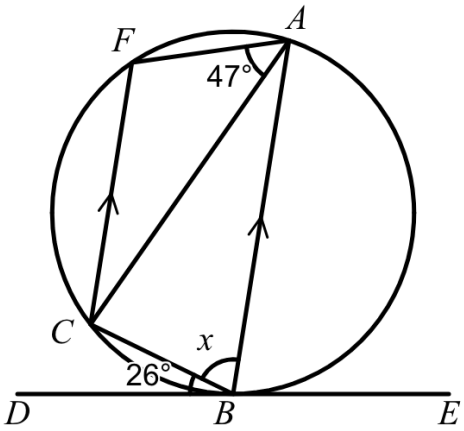


Dr Frost 442t

Worked Example

DE is a tangent to the circle at B

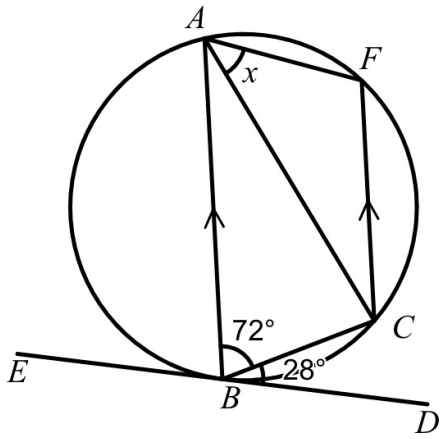
Find the value of x



Your Turn

DE is a tangent to the circle at B

Find the value of x

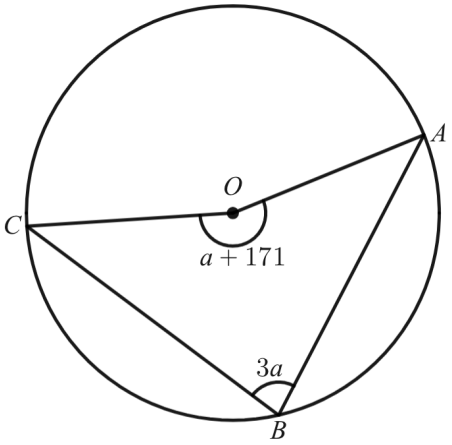


Worked Example

A, B and C are points on a circle, centre O

Angle $ABC = 3a$
Angle $AOC = a + 171$

Work out the value of a

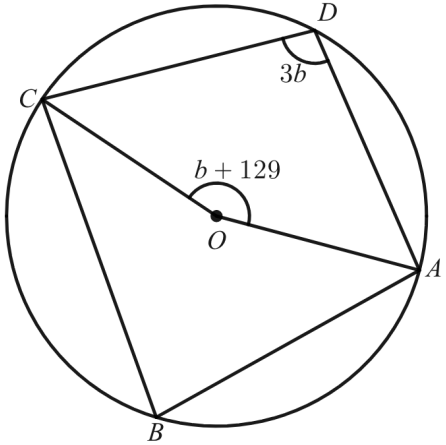


Your Turn

A, B and C are points on a circle, centre O

Angle $ADC = 3b$
Angle $AOC = b + 129$

Work out the value of b

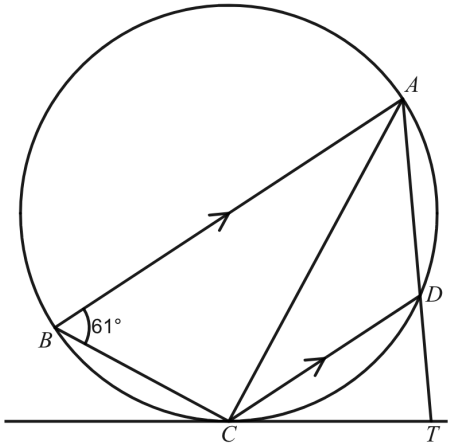


Worked Example

A, B, C and D are points on a circle.
AB is a diameter of the circle.
DC is parallel to AB
Angle $ABC = 61°$

The tangent to the circle at C meets the line AD extended at T

Calculate the size of angle ATC

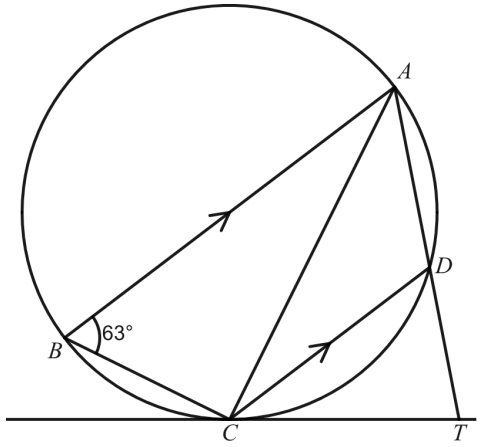


Your Turn

A, B, C and D are points on a circle.
AB is a diameter of the circle.
DC is parallel to AB
Angle $ABC = 63°$

The tangent to the circle at C meets the line AD extended at T

Calculate the size of angle ATC

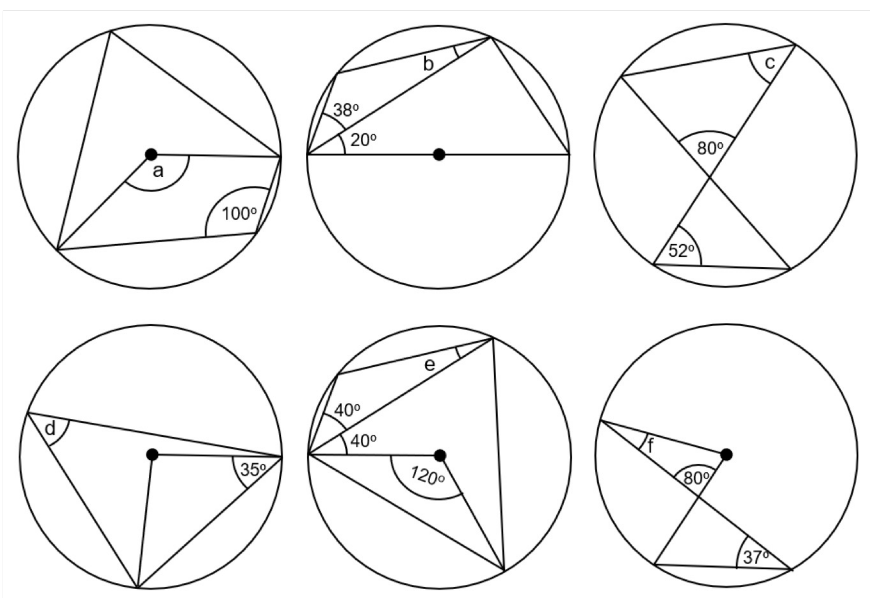


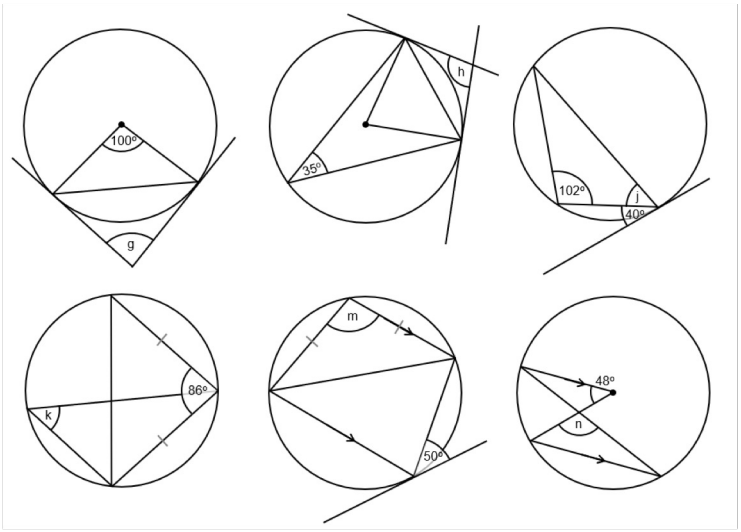
Fluency Practice

For the circle theorem questions after the grid, write your answers in the grid and tick all the angle facts you used in each case.

Compare your grid to your partner's grid - did you use the same methods? If not, explain your methods and see if they can follow your thinking.

Angle	Size	Angle Fact Used: Angle at the centre is twice the angle at the circumference	Angle in a semicircle is 90°	Opposite angles in a cyclic quadrilateral sum to 180°	Equal arcs subtend equal angles	Tangents to a point are equal	Tangent and radius meet at 90°	Alternate segment theorem	Base angles of an isosceles triangle are equal	Alternate angles are equal	Corresponding angles are equal	Vertically opposite angles are equal	Angles in a triangle sum to 180°	Angles on a straight line sum to 180°	Angles at a point sum to 360°
a															
b															
c															
d															
e															
f															
g															
h															
j															
k															
m															
n															



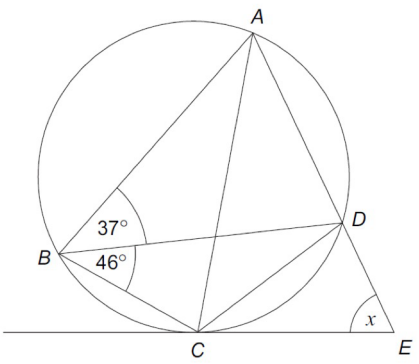


Incomplete Example:

For this question, the steps are given below, but the reasons are missing. Complete the table with the correct reasons, and label the calculated angles on the diagram.

The line joining C and E is a tangent to the circle

Not drawn accurately

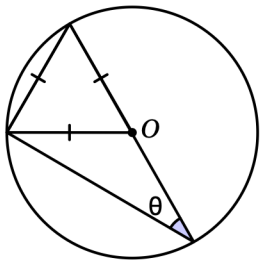


Work out the size of angle x.

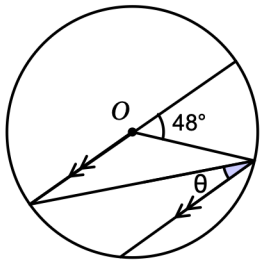
Step	Reason
Angle DCE = 46°	
Angle ACD = 37°	
Angle CAE = 46°	
$x = 180 - 46 - 46 - 37$	
$x = 51°$	-

1. Work out the angles marked θ.

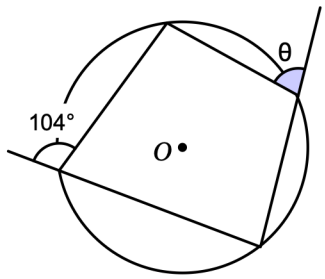
a)



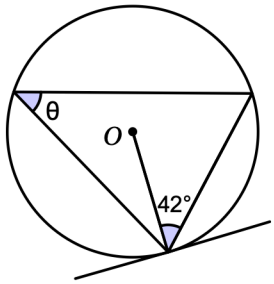
b)



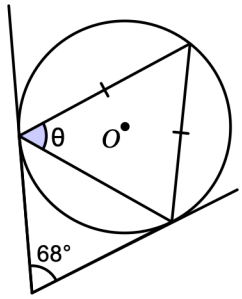
c)



d)



e)



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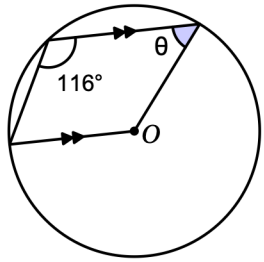
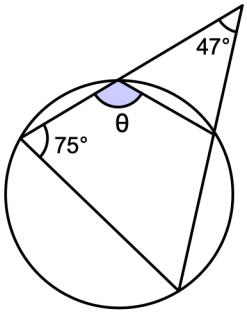
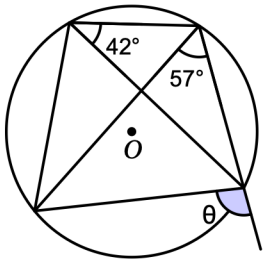


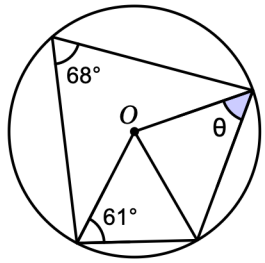
g)



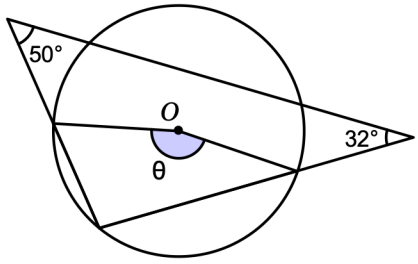
h)



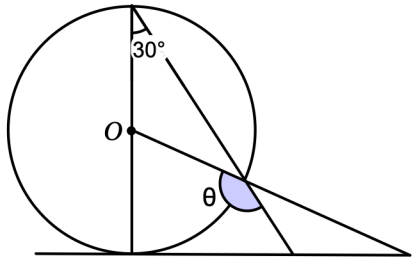
i)



j)

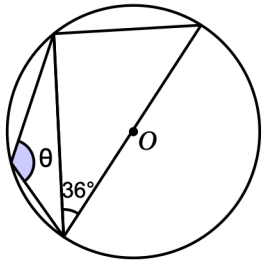


k)

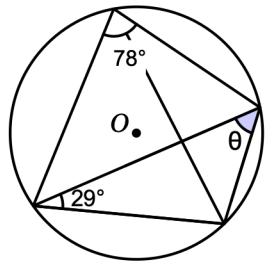


1. Work out the angles marked θ.

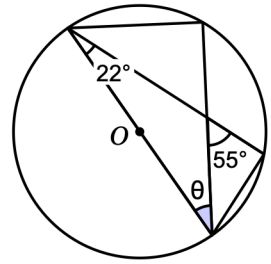
a)



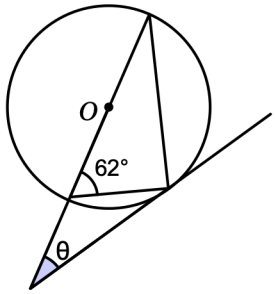
b)



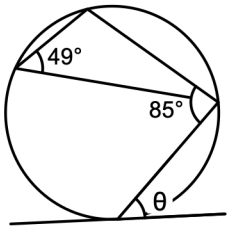
c)



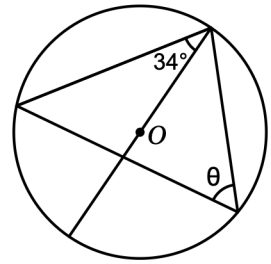
d)



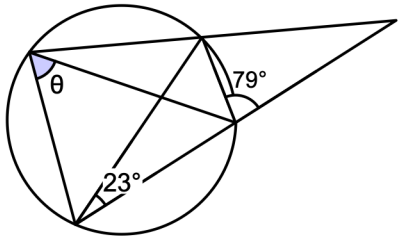
e)



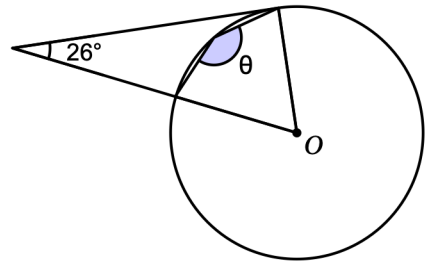
f)



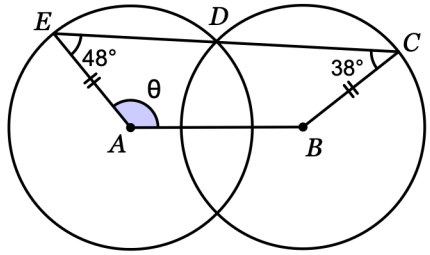
g)



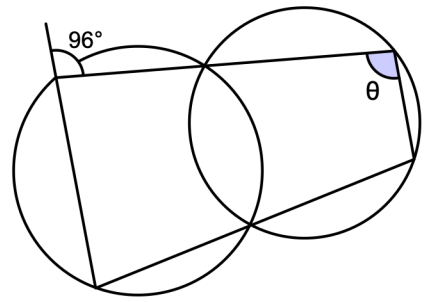
h)



i) A and B are the centres of the circles.
EDC is a straight line.
D lies on both circles.

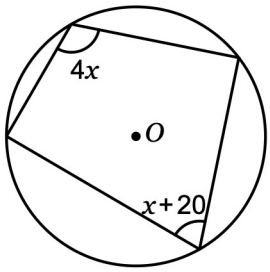


j)

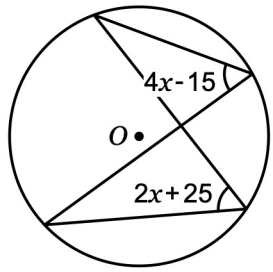


1. Work out value of x in each diagram:

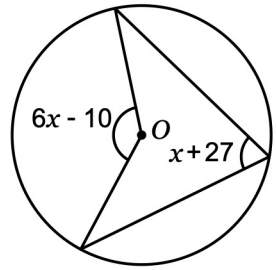
a)



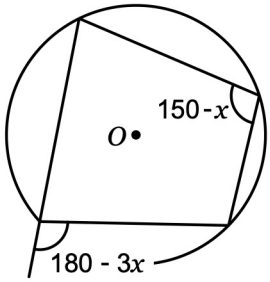
b)



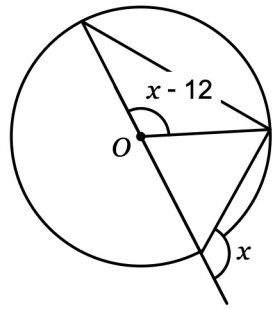
c)



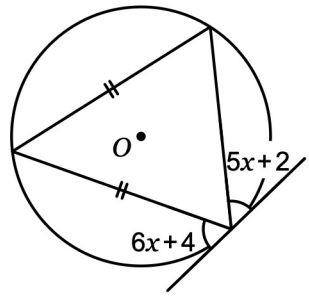
d)



e)

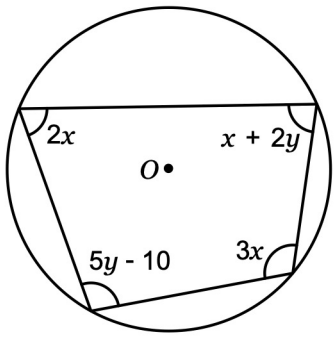


f)

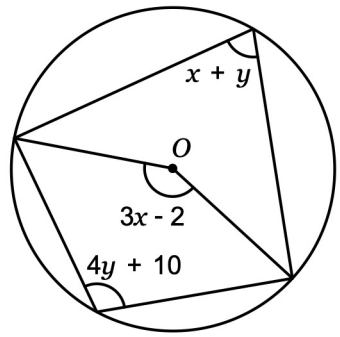


2. Work out values of x and y in each diagram:

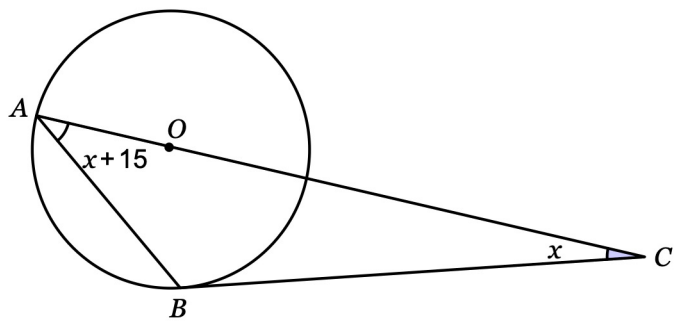
a)



b)

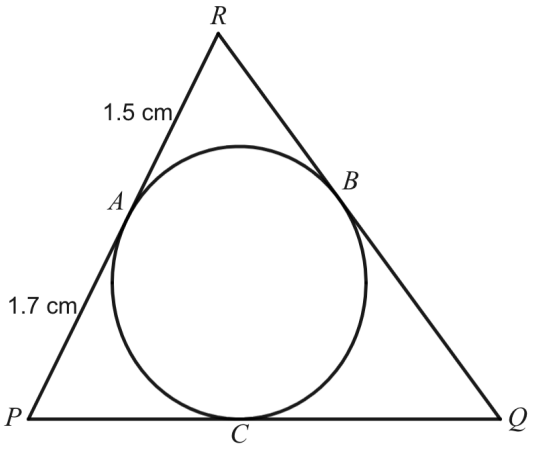


3. BC is a tangent to the circle.
Work out the value of x.



Worked Example

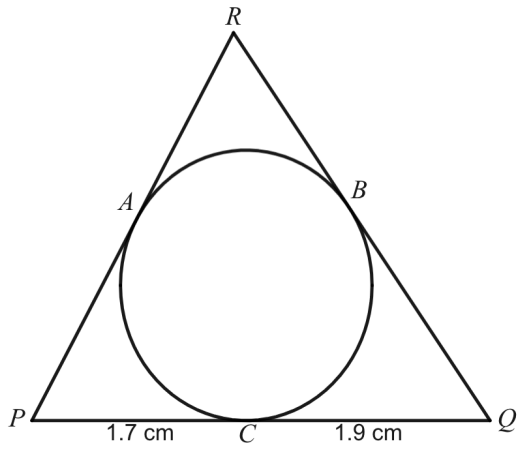
The sides of triangle PQR are tangents to a circle.
The tangents touch the circle at the points A, B and C
$RA = 1.5$ cm
$PA = 1.7$ cm



The perimeter of the triangle PQR is 10.6 cm
Work out the length of QB

Your Turn

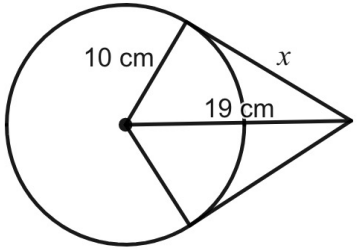
The sides of triangle PQR are tangents to a circle.
The tangents touch the circle at the points A, B and C
$PC = 1.7$ cm
$CQ = 1.9$ cm



The perimeter of the triangle PQR is 10.4 cm
Work out the length of RA

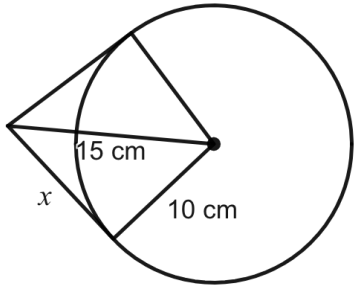
Worked Example

Find the value of x



Your Turn

Find the value of x



Extra Notes

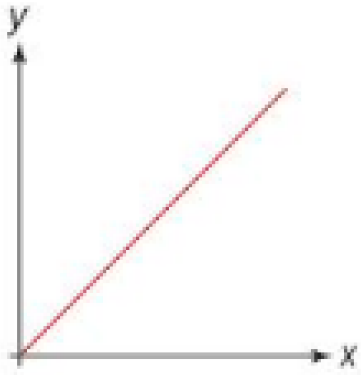
3 Direct and Inverse Proportion

Direct Proportion

y is directly proportional to x
y is proportional to x
y varies directly to x

$y \propto x$

$y = kx$
k is called the constant of proportionality



The graph of $y = kx$ is a straight line that passes through the origin.

Worked Example	Your Turn
y is directly proportional to x When $y = 20, x = 2$ a) Find y when $x = 5$ b) Find x when $y = 200$	b is directly proportional to a When $\mathrm{b} = 30, a = 5$ a) Find b when $\mathrm{a} = 2$ b) Find a when $b = 3000$

Worked Example	Your Turn
y is directly proportional to the square of x When $y = 36, x = 3$ a) Find y when $x = 5$ b) Find x when $y = 400$	b is directly proportional to the square of a When $\mathrm{b} = 12, a = 2$ a) Find b when $\mathrm{a} = 3$ b) Find a when $\mathrm{b} = 300$

Worked Example	Your Turn
y is directly proportional to the cube of x When $y = 32, x = 2$ a) Find y when $x = 5$ b) Find x when $y = 108$	b is directly proportional to the cube of a When $\mathrm{b} = 54, a = 3$ a) Find b when $\mathrm{a} = 4$ b) Find a when $\mathrm{b} = 16$

Worked Example	Your Turn
y is directly proportional to the square root of x When $y = 36, x = 16$ a) Find y when $x = 25$ b) Find x when $y = 900$	b is directly proportional to the square root of a When $\mathrm{b} = 36, a = 144$ a) Find b when $\mathrm{a} = 49$ b) Find a when $\mathrm{b} = 256$

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Worked Example

x is directly proportional to y^3
Complete the table.

y	-1	2	3	10
x	-2		54	

Your Turn

y is directly proportional to $\sqrt{p}$
Complete the table.

p	1	4	16	25	
y		8	16		24

Dr Frost 386i and 176f

Fill in the Gaps

General Statement	General Equation	Table of Values	Value of k	Specific Equation	When $x = 5$, $y =$?	When $y = 24$, $x =$?
$y \propto x$	$y = kx$	x: 1, 2, 10 / y: 3, ,	$k = 3$	$y = 3x$	$y = 3 \times 5$ $y = 15$	$24 = 3 \times x$ $x = 8$
$y \propto x$	$y = kx$	x: 1, 2, 10 / y: 8, , 80				$x = 3$
		x: 1, 2, 10 / y: , ,		$y = 2.5x$		$24 = 2.5 \times x$ $x = 9.6$
$y \propto x$		x: 1, 2, 10 / y: , 10,				
$y \propto x^2$	$y = kx^2$	x: 1, 2, 10 / y: , , 600	$k = 6$			$24 = 6 \times x^2$ $x = 2$
$y \propto x^2$		x: 1, 2, 10 / y: , , 150				
		x: 1, 2, 10 / y: , 1,	$k = 0.5$			

Fill in the Gaps

General Statement	General Equation	Table of Values	Value of k	Specific Equation
$y \propto x^3$	$y = kx^3$	x: 1, 2, 4 y: 3, ,	$k = 3$	
$y \propto \sqrt{x}$		x: 1, 4, 25 y: , 24,		
$y \propto x$		x: 1, 4, 10 y: , 3,		
	$y = k\sqrt[3]{x}$	x: 1, 8, 125 y: , 20,		
		x: 1, 4, 10 y: , 32, 200		
		x: 1, 4, y: , 3, 7.5	$k = 1.5$	
		x: 1, 4, y: , $\frac{32}{3}$, 24	$k = \frac{2}{3}$	
$y \propto x^3$		x: 2, $\sqrt{5}$, y: , 25, $27\sqrt{5}$		
		x: 1, 8, y: , $2a$, $4a$	$k = a$	

Fill in the Gaps

Direct Proportion – Method Breakdown Complete the table. Use the equation with the known constant (k) to answer the question.

Relationship in Words	Equation	Known Values	Substitution	Constant of Proportionality (k)	Equation Re-write	Question
y is directly proportional to x	$y = kx$	When x = 9, y = 45	$45 = k(9)$			When x = 10, y =
y is directly proportional to x squared	$y = kx^2$	When x = 3, y = 36	$36 = k(3)^2$			When x = 5, y =
y is directly proportional to x cubed		When x = 4, y = 128				When x = 3, y =
y is directly proportional to the square root of x	$y = k\sqrt{x}$	When x = 25, y = 15	$15 = k\sqrt{25}$			When x = 100, y =
	$y = k\sqrt[3]{x}$	When x = 8, y = 20				When x = 64, y =
	$y = kx$	When x = 5, y = 40				When x = 2.5, y =
y is directly proportional to x squared		When x = 4, y = 96				When x = 10, y =
y is directly proportional to the square root of x		When x = 81, y = 81				When x = 36, y =
		When x = 5, y = 500	$500 = k(5)^3$			When x = 3, y =
y is directly proportional to the cube root of x		When x = 1000, y = 70				When x = 8, y =
y is directly proportional to x		When x = 16, y = 56				When y = 49, x =
y is directly proportional to x squared		When x = 3, y = 4.5				When y = 72, x =
y is directly proportional to x cubed		When x = 2, y = 1.6				When y = 12.8, x =

Worked Example	Your Turn
y is directly proportional to $x + 2$ When $y = 20$, $x = 2$ Find y when $x = 5$	y is directly proportional to $x + 2$ When $y = 12$, $x = 2$ Find y when $x = 8$

Worked Example	Your Turn
y is directly proportional to $x^2 + 4$ When $y = 52$, $x = 3$ Find y when $x = 5$	y is directly proportional to $2x^2$ When $y = 36$, $x = 3$ Find y when $x = 5$

Inverse Proportion

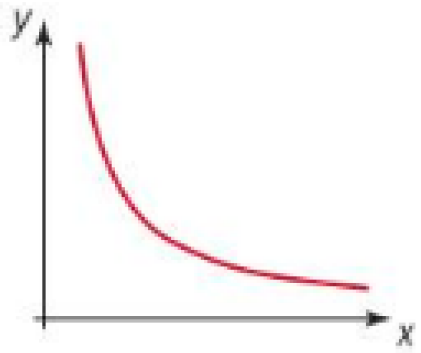
y is inversely proportional to x
y varies inversely or indirectly to x

$$y \propto \frac{1}{x}$$

$$y = \frac{k}{x}$$

k is called the constant of proportionality

The graph of $y = \frac{k}{x}$ is a reciprocal graph.



Worked Example	Your Turn
y is inversely proportional to x When $y = 5, x = 2$ a) Find y when $x = 5$ b) Find x when $y = 0.5$	b is inversely proportional to a When $\mathrm{b} = 10, a = 3$ a) Find b when $\mathrm{a} = 5$ b) Find a when $\mathrm{b} = 0.25$

Worked Example	Your Turn
y is inversely proportional to the square of x When $y = 6, x = 10$ a) Find y when $x = 5$ b) Find x when $y = 1.5$	b is inversely proportional to the square of a When $\mathrm{b} = 6, a = 5$ a) Find b when $\mathrm{a} = 10$ b) Find a when $\mathrm{b} = 6$

Worked Example	Your Turn
y is inversely proportional to the cube of x When $y = 8, x = 10$ a) Find y when $x = 2$ b) Find x when $y = 15.625$	b is inversely proportional to the cube of a When $\mathrm{b} = 5, a = 2$ a) Find b when $\mathrm{a} = 10$ b) Find a when $\mathrm{b} = 0.625$

Worked Example	Your Turn
y is inversely proportional to the square root of x When $y = 4, x = 25$ a) Find y when $x = 4$ b) Find x when $y = 2.5$	b is inversely proportional to the square root of a When $\mathrm{b} = 4, a = 9$ a) Find b when $\mathrm{a} = 16$ b) Find a when $\mathrm{b} = 6$

Dr Frost 386d and 386f

Worked Example

Given that x is inversely proportional to the square root of z
Complete the table.

z	36		25
x	16	24	

Your Turn

Given that b is inversely proportional to y^3
Complete the table.

y	4	12	
b	3375		216

Dr Frost 386j and 176o

Fill in the Gaps

General Statement	General Equation	Table of Values	Value of k	Specific Equation	When $x = 6$, $y =$?	When $y = 10$, $x =$?
$y \propto \frac{1}{x}$	$y = \frac{k}{x}$	x: 1, 4, 8 y: 48, ,	$k = 48$	$y = \frac{48}{x}$	$y = \frac{48}{6} = 8$	$x = \frac{48}{10} = 4.8$
$y \propto \frac{1}{x}$	$y = \frac{k}{x}$	x: 1, 2, 5 y: 120, , 24				$x = \frac{120}{10} = 12$
		x: 1, 5, 10 y: , ,		$y = \frac{30}{x}$		$x = \frac{30}{10} = 3$
$y \propto \frac{1}{x}$		x: 5, 20, 100 y: , 30,				
$y \propto \frac{1}{x^2}$	$y = \frac{k}{x^2}$	x: 1, 2, 3 y: , , 40	$k = 360$			$x = \sqrt{\frac{360}{10}} = 6$
$y \propto \frac{1}{x^2}$		x: 1, 2, 10 y: , , 3				
		x: 1, 5, 10 y: , 4,	$k = 20$			

Fill in the Gaps

General Statement	General Equation	Table of Values	Value of k	Specific Equation
$y \propto \frac{1}{x^2}$	$y = \frac{k}{x^2}$	x: 1, 2, 5 y: 100, ,	$k = 100$	
$y \propto \frac{1}{\sqrt{x}}$		x: 1, 4, 25 y: , 5,		
$y \propto \frac{1}{x^3}$		x: 1, 2, 10 y: , 125,		
	$y = \frac{k}{\sqrt[3]{x}}$	x: 1, 8, 125 y: , 20,		
		x: 1, 4, 10 y: , 7.5, 3		
		x: 1, 2, y: , 0.75, 0.12	$k = 3$	
		x: 1, 4, y: , $\frac{1}{12}$, $\frac{1}{30}$	$k = \frac{1}{6}$	
$y \propto \frac{1}{x^3}$		x: 1, $\sqrt{3}$, 2 y: , 3,		
		x: 0.5, 2, y: $4a$, , $\frac{a}{16}$	$k = a$	

Fill in the Gaps

Inverse Proportion – Method Breakdown Complete the table. Use the equation with the known constant (k) to answer the question.

Relationship in Words	Equation	Known Values	Substitution	Constant of Proportionality (k)	Equation Re-write	Question
y is inversely proportional to x	$y = \frac{k}{x}$	When x = 8, y = 2	$2 = \frac{k}{8}$			When x = 2, y =
y is inversely proportional to x squared		When x = 4, y = 0.5	$0.5 = \frac{k}{(4)^2}$			When x = 2, y =
	$y = \frac{k}{x^3}$	When x = 2, y = 5				When x = 1, y =
	$y = \frac{k}{\sqrt{x}}$	When x = 25, y = 4				When x = 100, y =
		When x = 8, y = 4	$4 = \frac{k}{\sqrt[3]{8}}$			When x = 64, y =
y is inversely proportional to x		When x = 2, y = 2.5				When x = 20, y =
y is inversely proportional to x cubed		When x = 4, y = 0.25				When x = 10, y =
y is inversely proportional to the square root of x		When x = 100, y = 3				When x = 9, y =
y is inversely proportional to the cube root of x		When x = 125, y = 10				When x = 8, y =
y is inversely proportional to x squared		When x = 10, y = 2				When x = 5, y =

Worked Example	Your Turn
y is inversely proportional to $x + 3$ When $y = 52$, $x = 3$ Find y when $x = 5$	y is inversely proportional to $2x + 1$ When $y = 30$, $x = 4$ Find y when $x = 7$

Fill in the Gaps

Type	**Statement**	k-Formula	k value x = 2 , y = 4	Final Formula
y is proportional to x	$y \propto x$	$y = k\,x$		
x is proportional to y				
y is inversely proportional to x	$y \propto \frac{1}{x}$	$y = \frac{k}{x}$		
x is inversely proportional to y				
y is proportional to the square of x				
x is proportional to the square of y				
x is proportional to $\sqrt{y}$				
Y is inversely proportional to $\sqrt{x}$				
Y is proportional to x^3				
x is proportional to 3 more than y				

Fill in the Gaps

Direct & Inverse Proportion – Method Breakdown Complete the table. Use the equation with the known constant (k) to answer the question.

Relationship in Words	Equation	Known Values	Substitution	Constant of Proportionality (k)	Equation Re-Write	Question
y is directly proportional to x	$y = kx$	When x = 9, y = 45	$45 = k(9)$			When x = 10, y =
y is inversely proportional to x	$y = \frac{k}{x}$	When x = 8, y = 2				When x = 2, y =
y is directly proportional to x squared		When x = 3, y = 36	$36 = k(3)^2$			When x = 5, y =
	$y = kx^3$	When x = 4, y = 128				When x = 3, y =
	$y = \frac{k}{x^2}$	When x = 4, y = 0.5				When x = 2, y =
y is inversely proportional to x cubed		When x = 2, y = 5				When x = 1, y =
y is directly proportional to the square root of x	$y = k\sqrt{x}$	When x = 25, y = 15				When x = 100, y =
	$y = k\sqrt[3]{x}$	When x = 8, y = 20				When x = 64, y =
	$y = \frac{k}{\sqrt{x}}$	When x = 25, y = 4				When x = 100, y =
y is inversely proportional to the cube root of x		When x = 8, y = 4				When x = 64, y =
y is directly proportional to x squared		When x = 3, y = 4.5				When y = 72, x =
y is inversely proportional to the square root of x		When x = 100, y = 3				When x = 9, y =

Worked Example

m	16	25
n	625	256

Select the correct statement below.

- ○ $n \propto \frac{1}{\sqrt{m}}$
- ○ $n \propto \frac{1}{m}$
- ○ $n \propto \frac{1}{m^2}$

Your Turn

c	1	4
d	32	2

Select the correct statement below.

- ○ $d \propto \frac{1}{\sqrt{c}}$
- ○ $d \propto \frac{1}{c}$
- ○ $d \propto \frac{1}{c^2}$

Dr Frost 386k and 176p

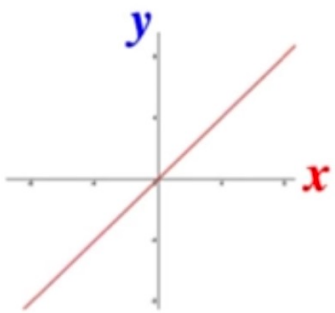
Worked Example	Your Turn
x is inversely proportional to y^2 y is directly proportional to $\sqrt[3]{z}$ Given that $x = 10$ and $z = 512$ when $y = 7$ find a formula for x in terms of z	x is directly proportional to y^3 y is inversely proportional to $\sqrt{z}$ Given that $x = 10$ and $z = 36$ when $y = 5$ find a formula for x in terms of z

Worked Example	Your Turn
q is proportional to t^3 t is decreased by 30% Work out the percentage decrease in q	y is proportional to z^2 z is decreased by 80% Work out the percentage decrease in y

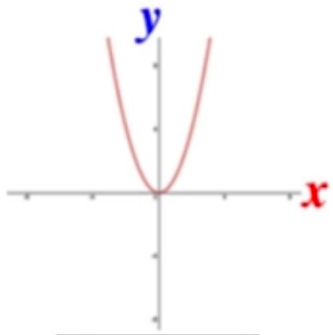
Worked Example	Your Turn
t is inversely proportional to z^3 z is decreased by 50% Find the percentage increase in t	y is inversely proportional to p^2 p is decreased by 50% Find the percentage increase in y

Worked Example	Your Turn
r is inversely proportional to s^2 $r = 34$ when $s = 3d$ Find r when $s = d$	y is inversely proportional to x^3 $y = 99$ when $x = 2c$ Find y when $x = 3c$

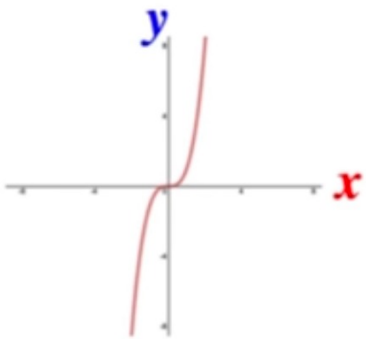
Graphs



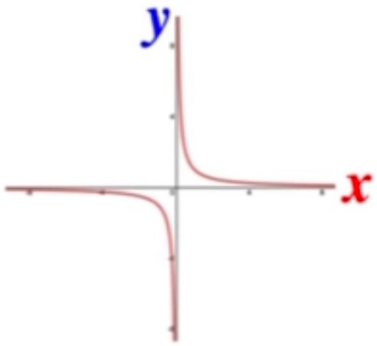
$y = kx$



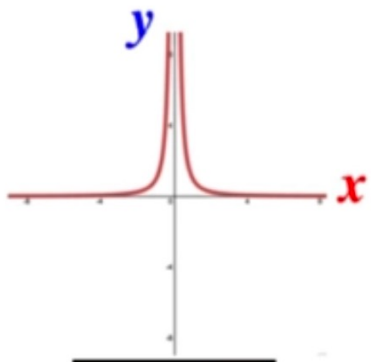
$y = kx^2$



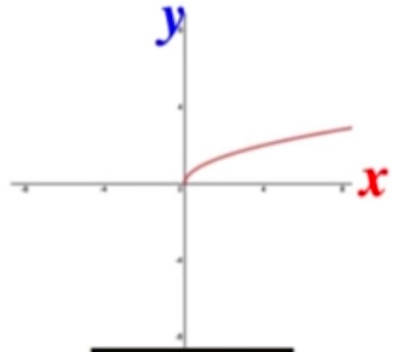
$y = kx^3$



$y = \frac{k}{x}$



$y = \frac{k}{x^2}$

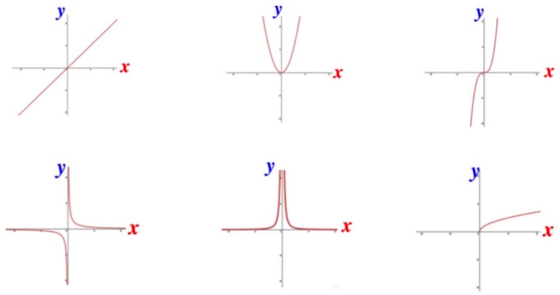


$y = k\sqrt{x}$

Fluency Practice

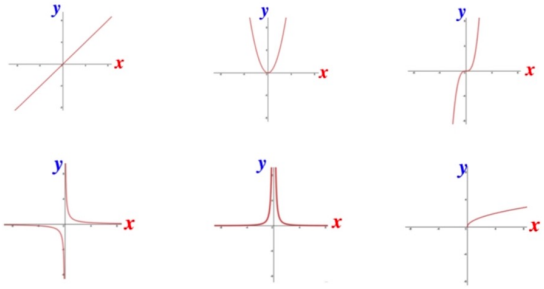
y is proportional to the square of x

Which of the following could be the graph demonstrating between y and x?



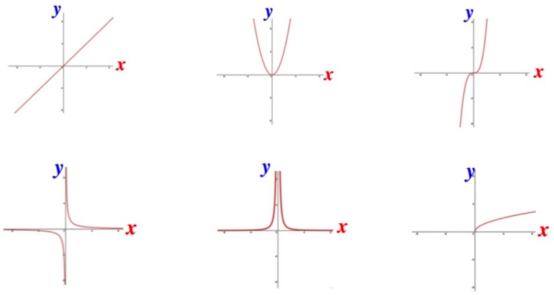
$y \propto x$

Which of the following could be the graph demonstrating between y and x?



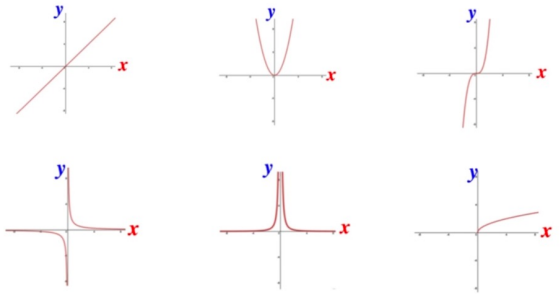
y is inversely proportional to x

Which of the following could be the graph demonstrating between y and x?



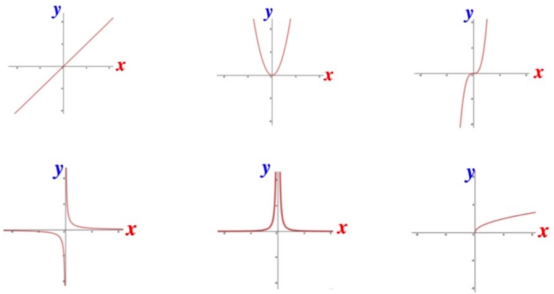
$y \propto x^3$

Which of the following could be the graph demonstrating between y and x?



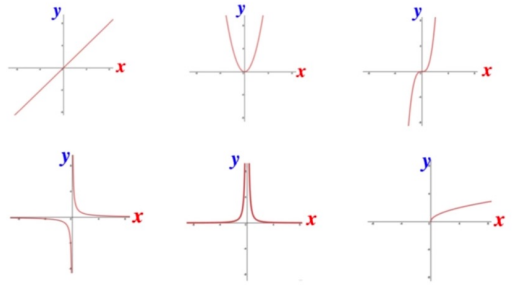
y is inversely proportional to the square of x

Which of the following could be the graph demonstrating between y and x?



$y \propto \sqrt{x}$

Which of the following could be the graph demonstrating between y and x?

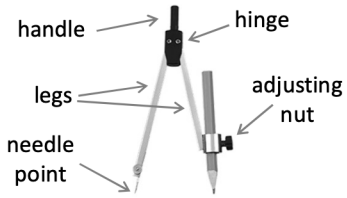


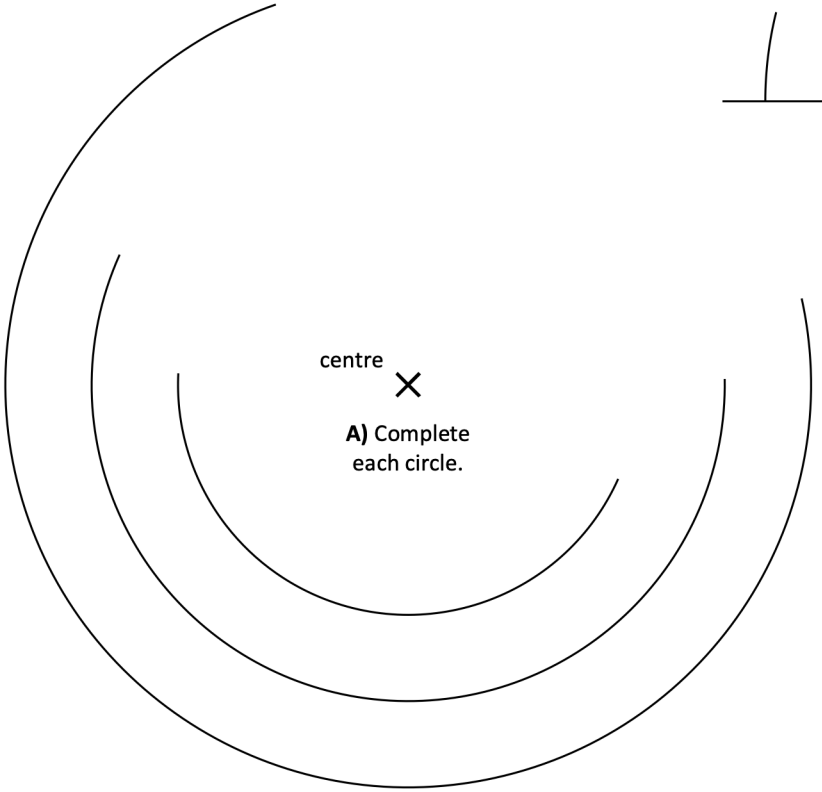
Extra Notes

4 Constructions and Loci

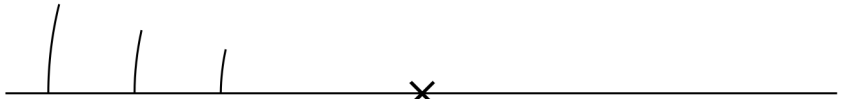
Fluency Practice

Compass Skills

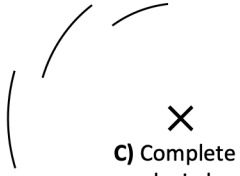




A) Complete each circle.



B) Complete each semicircle.



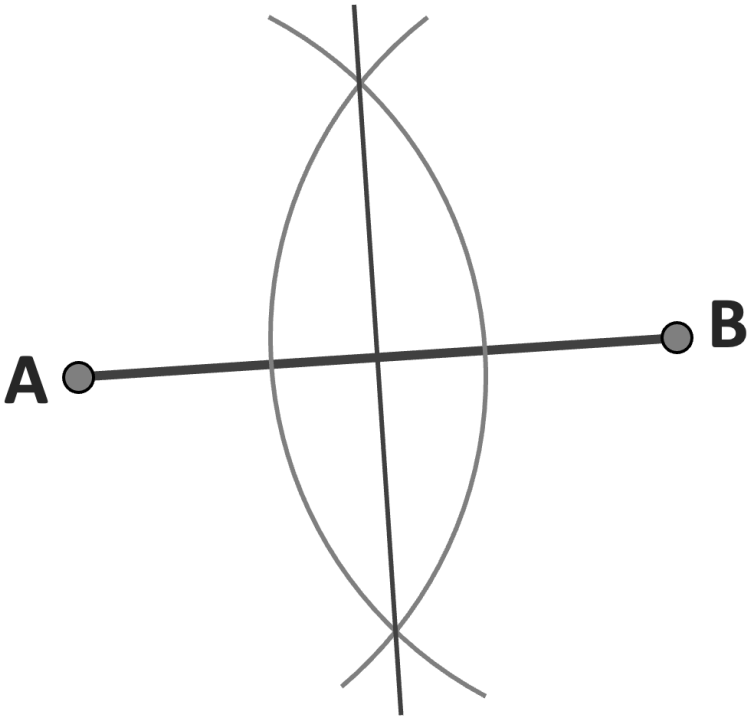
C) Complete each circle.

Quick Tips:
When the compass is closed, the point and the pencil point should meet.
Make sure the legs are not loose (this needs tight hinge screws).
Place paper underneath the worksheet to make the point hold.
When drawing, try to only hold the handle with a finger and thumb.

Perpendicular Bisector

Draw two points on your page and label them A and B.
Join them with a straight line.
Construct its perpendicular bisector.

1) Draw two equal arcs.
2) Connect the intersections with a straight line.
3) This line is the perpendicular bisector and contains all the points equidistant from A and B.



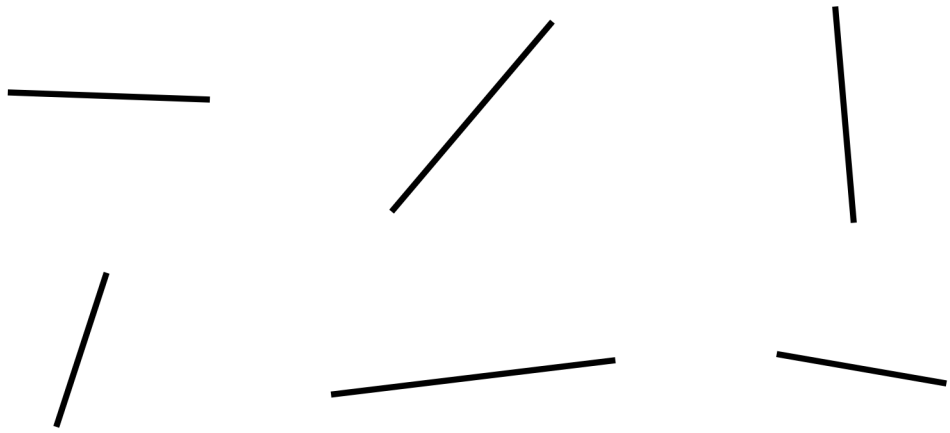
Worked Example

Construct the perpendicular bisector of the line:

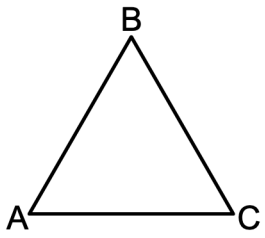
Your Turn

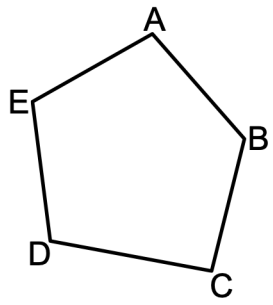
Construct the perpendicular bisector of the line:

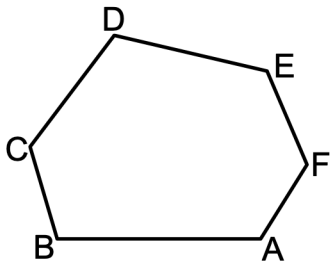
Q1 Construct the perpendicular bisector of the following lines.

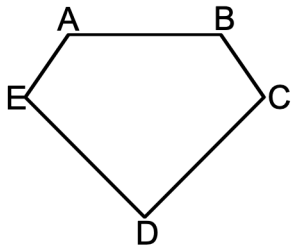


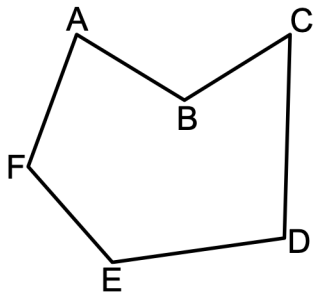
Q2 Construct the perpendicular bisector of the line **AB** in each of the following.

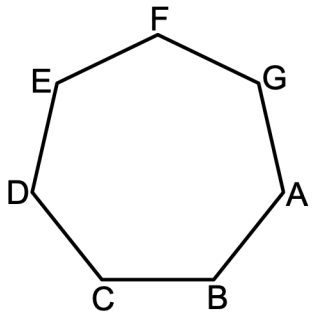








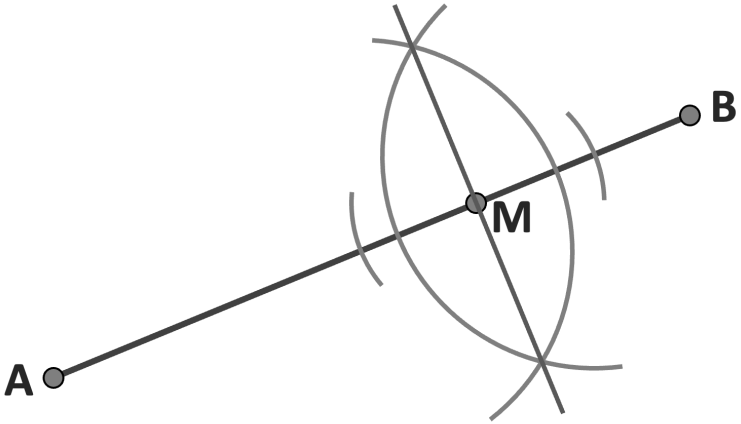




Perpendicular Line at a Point 1

M is a point on the line AB.
Construct a line perpendicular to AB through M.

1) Use your compass to find two points on the line equidistance from M.
2) Construct a perpendicular bisector of these two points.



Worked Example

Construct a perpendicular to the line which passes through the marked point:

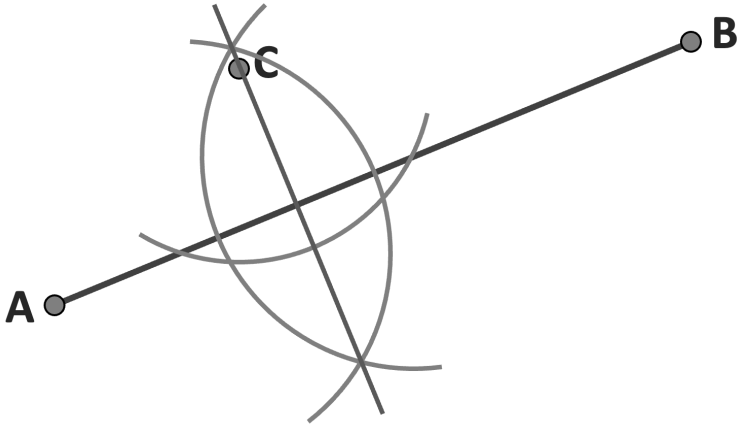
Your Turn

Construct a perpendicular to the line which passes through the marked point:

Perpendicular Line at a Point 2

Construct a line perpendicular to AB through C, which is a point not on AB.

1) Use your compass to find two points on the line equidistance from C.
2) Construct a perpendicular bisector of these two points.



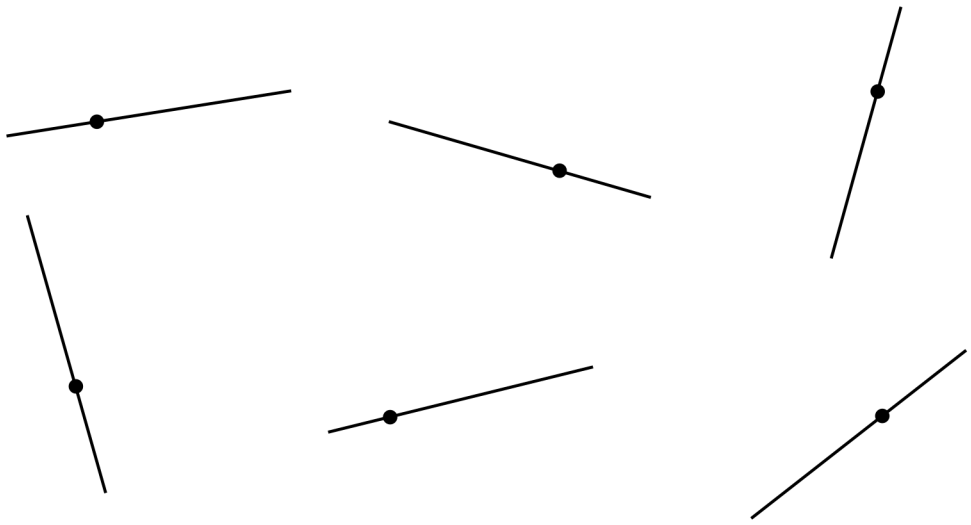
Worked Example

Construct a perpendicular to the line which passes through the marked point:

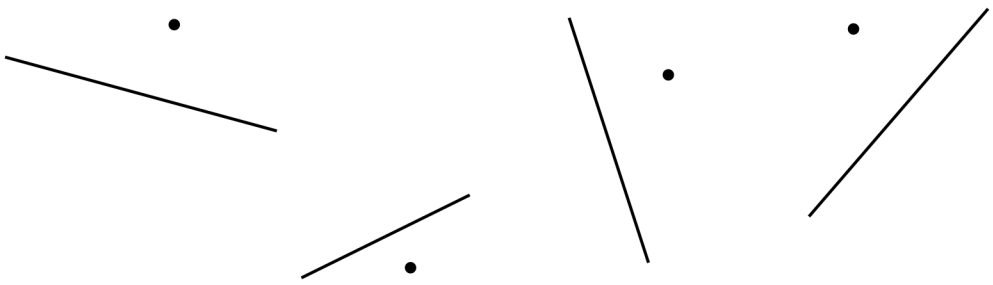
Your Turn

Construct a perpendicular to the line which passes through the marked point:

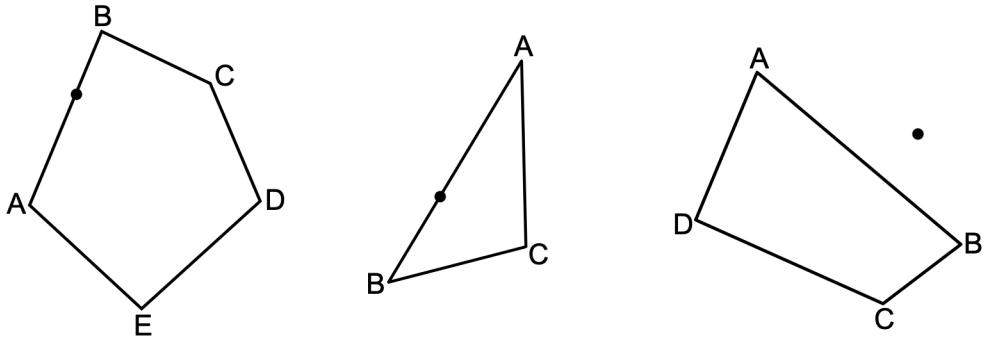
Q3 Construct the perpendicular bisector of the following lines through the given point.



Q4 Construct the perpendicular bisector of the following lines through the given point.



Q5 Construct the perpendicular bisector of the line **AB** through the given point.



Angle Bisector

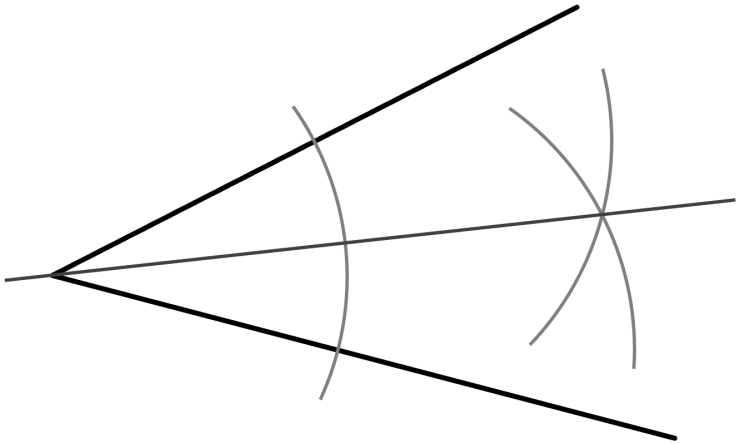
Draw an acute angle on your page.
Construct its angle bisector.

1) Draw an arc from the vertex.

2) Draw two more equal arcs from the intersections.

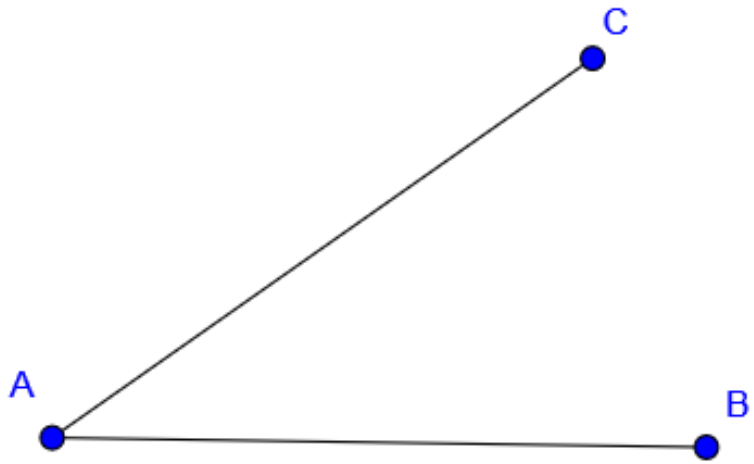
3) Join the new intersection up to the vertex.

4) This line is the angle bisector and contains all points equidistant from both arms of the angle.



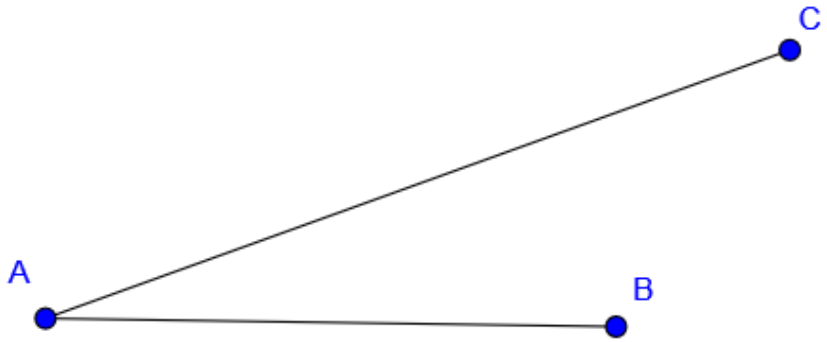
Worked Example

Bisect angle BAC:

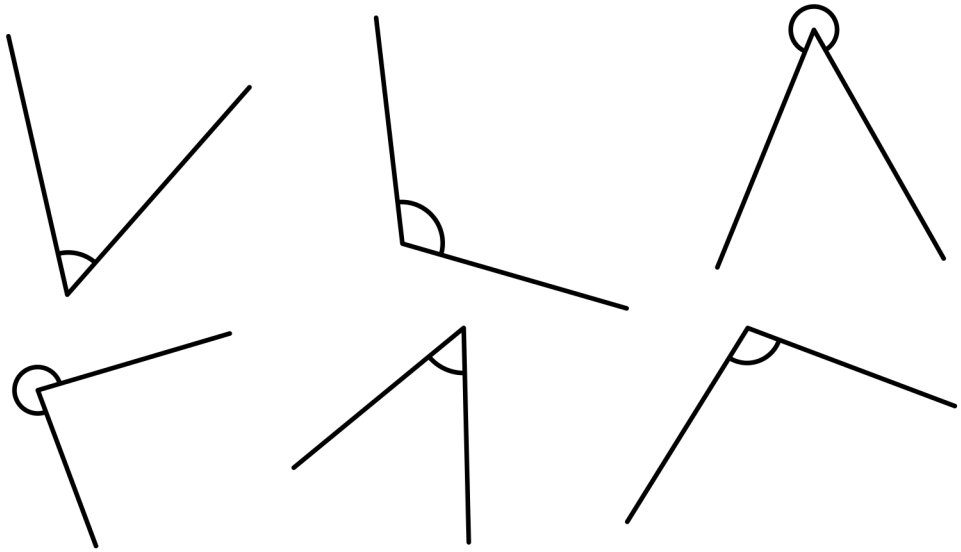


Your Turn

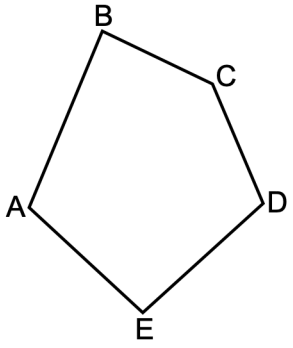
Bisect angle BAC:

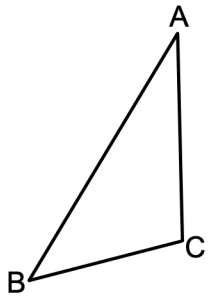


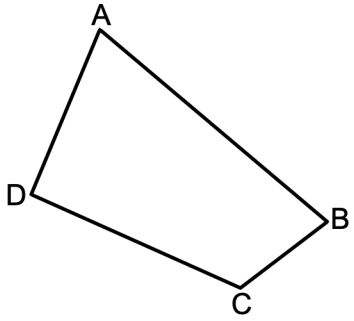
Q6 Construct the **angle bisector** of the following angles.



Q7 Construct the angle bisector of ∠**ABC** for each of the following shapes..







Q8 Construct a 90^{o} angle.

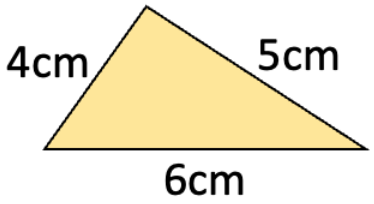
Q9 Construct a 45`^{o} angle.

Constructing Triangles

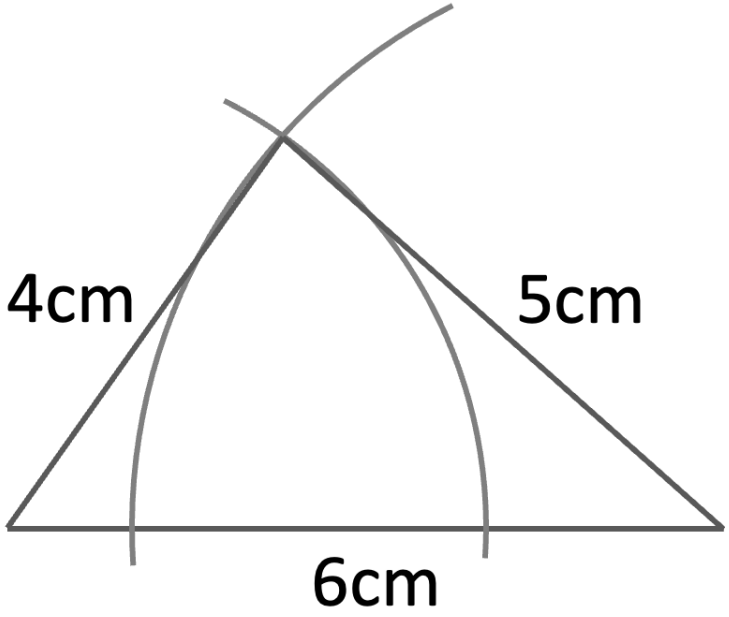
You can construct a unique triangle when you know:
Two sides and the angle between them **(SAS)**
Two angles and a side **(ASA)**
Three sides **(SSS)**

SSS

Using a ruler and compass only, construct the following SSS triangle accurately.



1) Draw a 6cm line with a ruler.
2) Draw two arcs with lengths 4cm and 5cm from each end of the line.
3) Join the ends of the line to the intersection.



Worked Example

Construct a triangle with:

- A side length of $10\ cm$
- A side length of $6\ cm$
- A side length of $8\ cm$

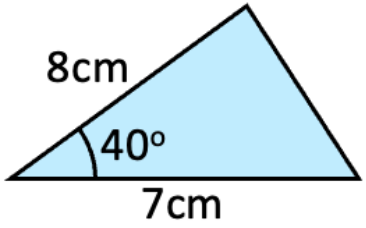
Your Turn

Construct a triangle with:

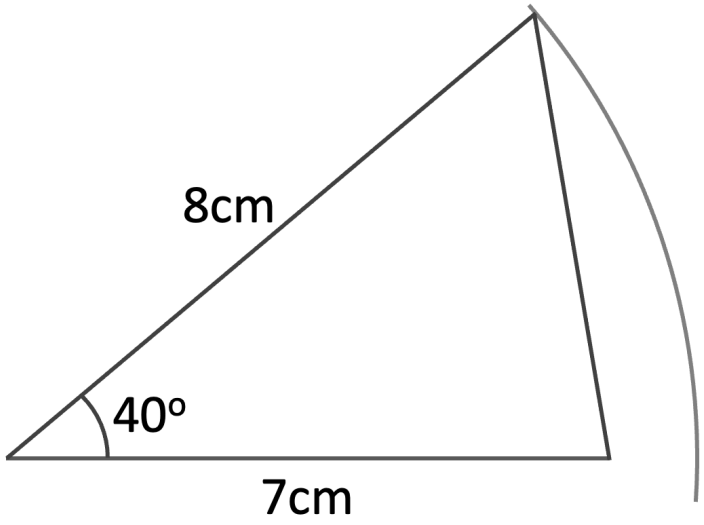
- A side length of $5\ cm$
- A side length of $3\ cm$
- A side length of $4\ cm$

SAS

Using a ruler, compass and protractor, construct the following SAS triangle accurately.



1) Draw a 7cm line with a ruler.
2) Draw an arc with length 8cm.
3) Measure an angle of 40°.
4) Draw a line through the angle to the arc.
5) Join up the end of the lines.



Worked Example

Construct a triangle with:

- A side length of $10\ cm$
- An angle of $30°$
- A side length of $8\ cm$

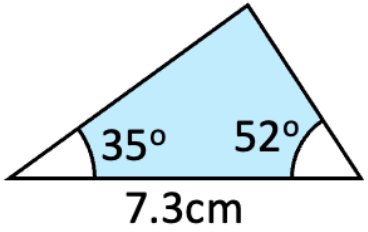
Your Turn

Construct a triangle with:

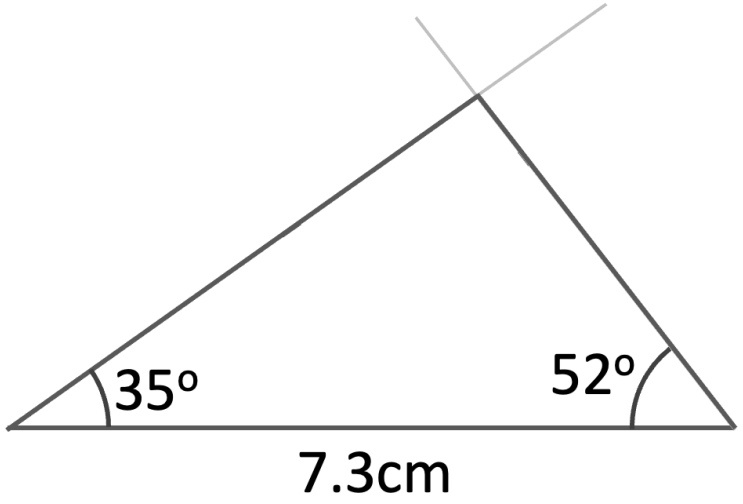
- A side length of $5\ cm$
- An angle of $30°$
- A side length of $4\ cm$

ASA

Using a ruler, compass and protractor, construct the following ASA triangle accurately.



1) Draw a 7.3cm line with a ruler.
2) Measure both angles.
3) Draw a feint line through each angle and label them.
4) Draw a solid line over each feint line up to the intersection.



Worked Example

Construct a triangle with:

- An angle of $30°$
- A side length of $10\ cm$
- An angle of $45°$

Your Turn

Construct a triangle with:

- An angle of $30°$
- A side length of $5\ cm$
- An angle of $60°$

Loci

Worked Example

Construct the locus of points $1\ cm$ away from a point.

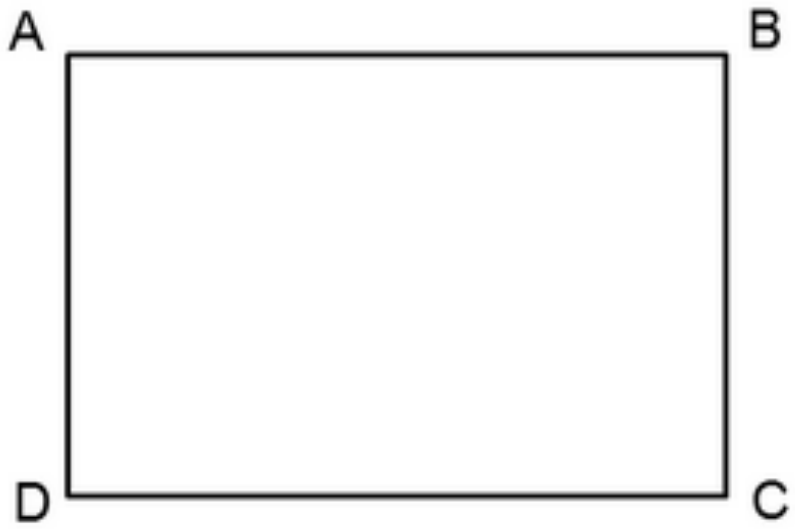
Your Turn

Construct the locus of points $2\ cm$ away from a point.

Worked Example

Construct the locus of points which is:

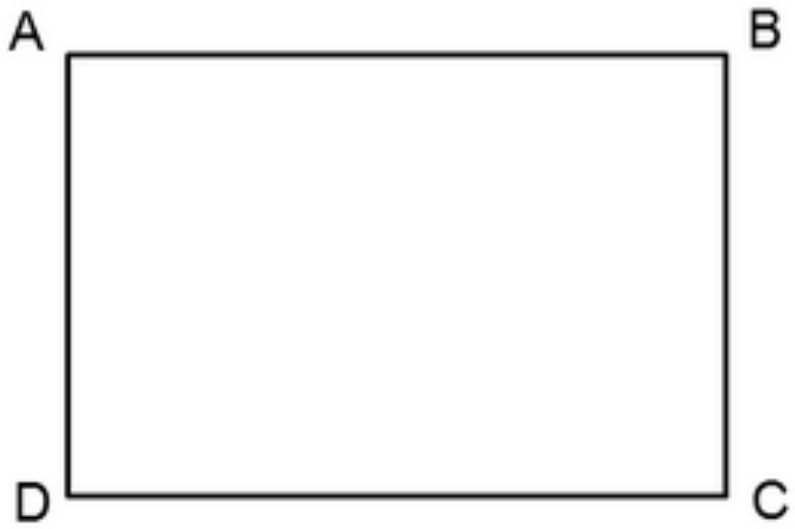
- More than $3\ cm$ from A



Your Turn

Construct the locus of points which is:

- More than $5\ cm$ from B



Worked Example

Construct the locus of points equidistant from two points.

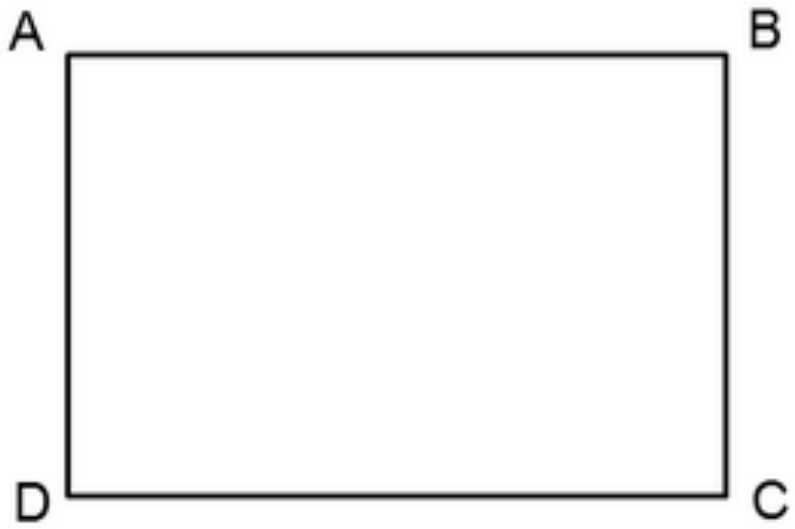
Your Turn

Construct the locus of points equidistant from two points.

Worked Example

Construct the locus of points which are:

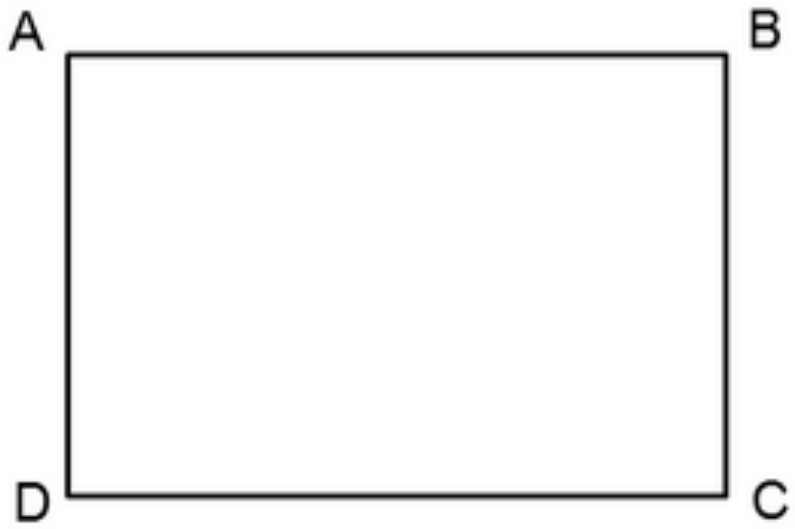
- Closer to B than A
- Closer to C than D



Your Turn

Construct the locus of points which are:

- Closer to C than B
- Closer to D than A



Worked Example

Construct the locus of points equidistant from two intersecting lines.

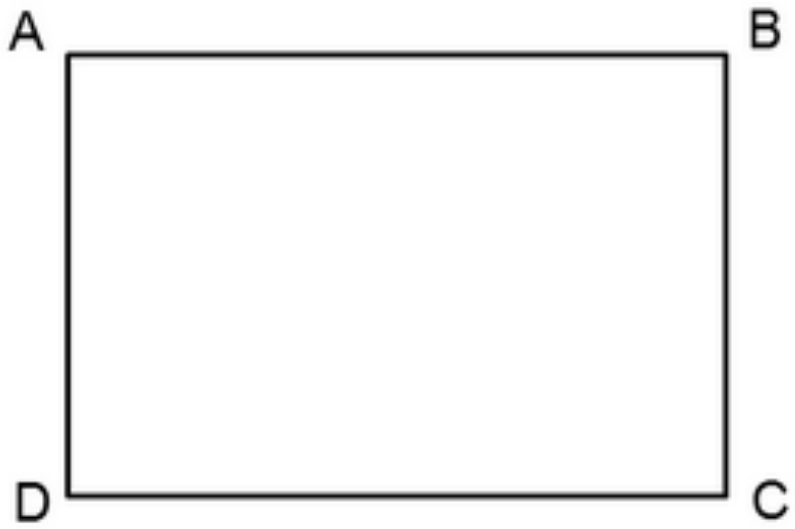
Your Turn

Construct the locus of points equidistant from two intersecting lines.

Worked Example

Construct the locus of points which is:

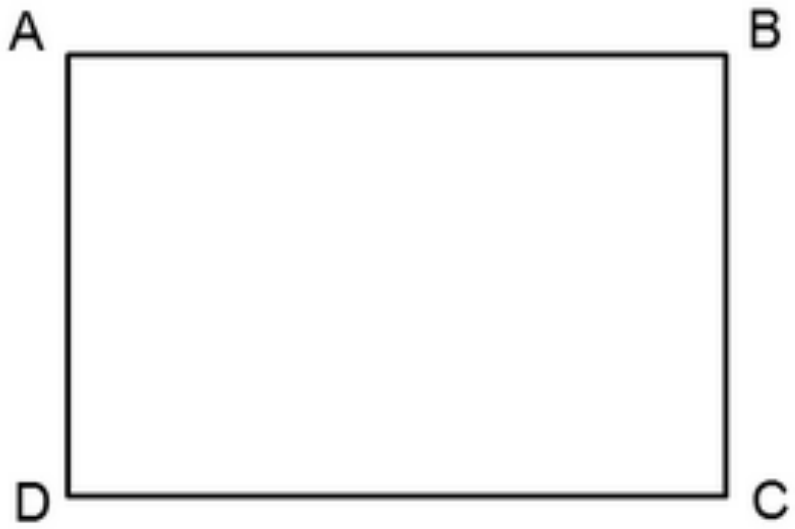
- Closer to AD than AB



Your Turn

Construct the locus of points which is:

- Closer to BC than DC



Worked Example

Construct the locus of points $1\ cm$ away from the line.

Your Turn

Construct the locus of points $1\ cm$ away from the line.

Worked Example

Construct the locus of points equidistant from a line.

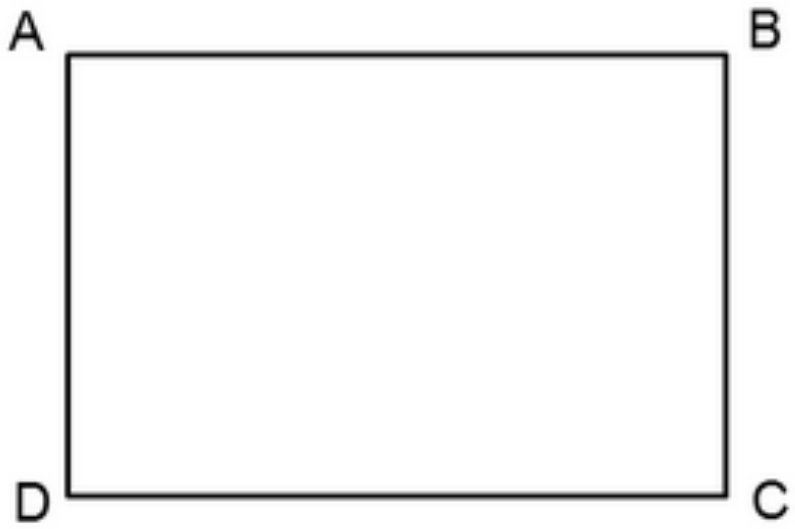
Your Turn

Construct the locus of points equidistant from a line.

Worked Example

Construct the locus of points which are:

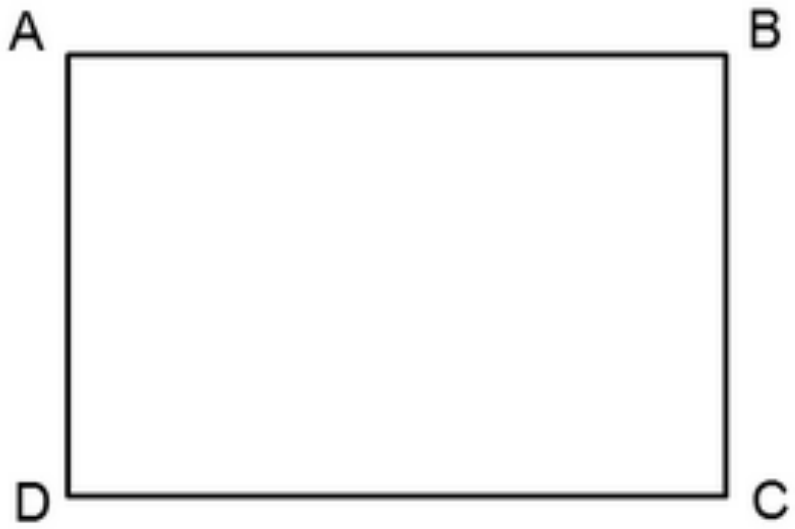
- More than $3\ cm$ from AB
- More than $4\ cm$ from AD



Your Turn

Construct the locus of points which are:

- More than $5\ cm$ from AB
- More than $3\ cm$ from AD



Worked Example

Construct the locus of points which are:

- Closer to B than C
- More than $3\ cm$ from A

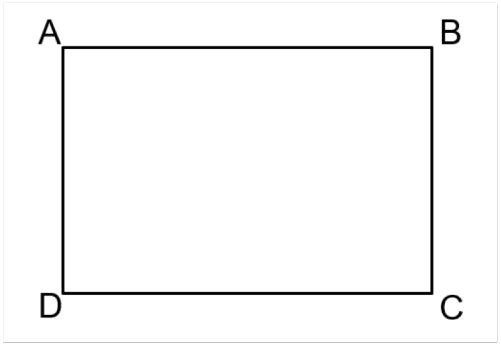
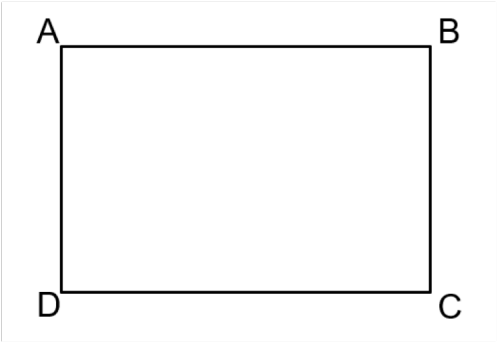
Your Turn

Construct the locus of points which are:

- Closer to C than A
- Less than $5\ cm$ from B

Fluency Practice

Loci and Regions – Shade the region inside the rectangle which satisfies the conditions given.

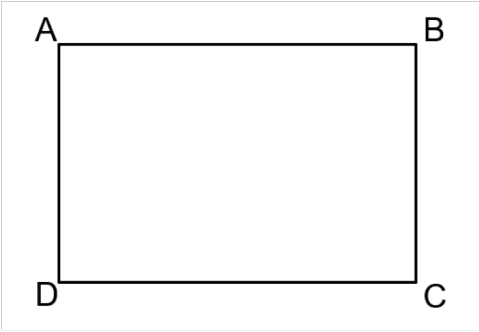
(a)	(b)	(c)
Less than 3 cm from A 	More than 3 cm from D 	More than 2 cm from AB 
(d)	**(e)**	**(f)**
Less than 3 cm from BC 	Closer to AB than AD 	Closer to A than B 

Fluency Practice

Harder Loci and Regions – Shade the region inside the rectangle which satisfies the conditions given.

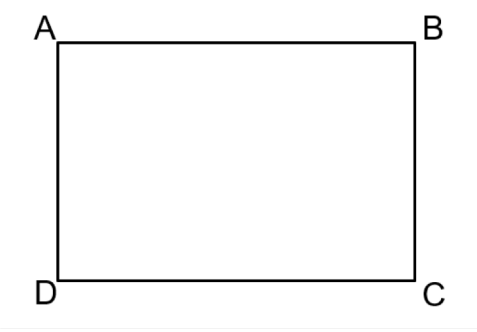
(a)

Less than 3 cm from A and more than 2 cm from AB



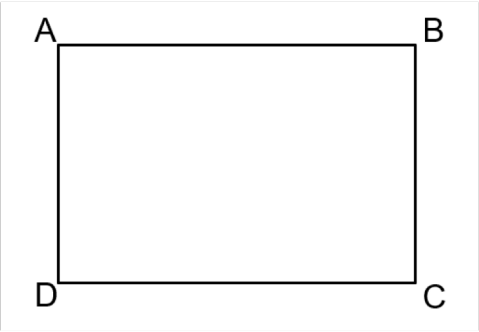
(b)

More than 3 cm from B and closer to AB than BC



(c)

Closer to AD than AB and less than 2 cm from AB

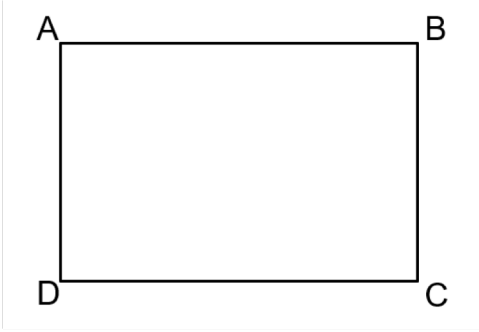


(d)

Less than 3 cm from BC and less than 2 cm from CD

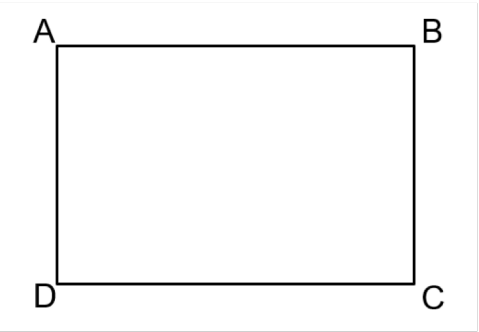
(e)

Closer to A than B and more than 4 cm from A

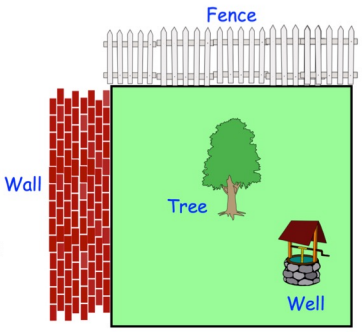


(f)

More than 3 cm from D and more than 4 cm from B



*There is a template for each question at the end of this exercise



Question 1:

The diagram shows Lindsey's garden.
Lindsey is deciding where to place a bench

Show the possible positions of the bench for each rule below

(a) The bench is 1 metre away from the wall.
(b) The bench is less than 2 metres away from the fence.
(c) The bench is 2 metres away from the tree.
(d) The bench is less than 2.5 metres away from the tree.
(e) The bench is an equal distance (equidistant) from the tree and the well.
(f) The bench is closer to the well than the tree.
(g) The bench is an equal distance from the wall and the fence
(h) The bench is closer to the wall than the fence.
(i) The bench is less than 2 metres from the wall **and** less than 3 metres from the tree
(j) The bench is closer to the fence than the wall **and** more than 1 metre from the wall.

Question 2:

Shown is a map of an island.
Show the possible position of each item.

(a) The stadium is equidistant from Redville and Newtown

(b) A ship is less than 2 miles from the harbour

(c) A helicopter is 6 miles from the harbour **and** 4 miles from the airport.

(d) A church is closer to Redville than Newtown **and** is more than 3 miles from the airport

(e) A lighthouse is equidistant from Newtown and the harbour **and** is on the coast.

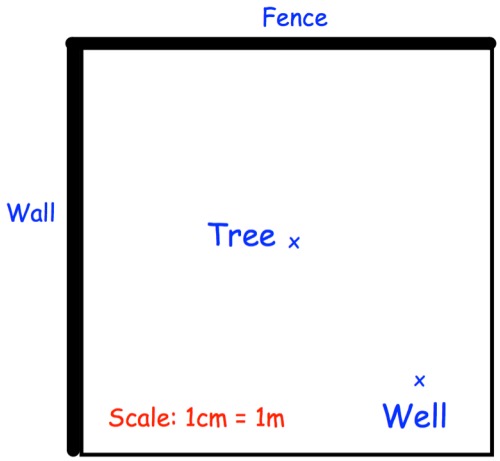
(f) A windmill is less than 4 miles from Redville **and** less than 4 miles from Newtown **and** less than 4 miles from the Airport.

(g) A hot air balloon is between 5 miles and 7 miles from the harbour

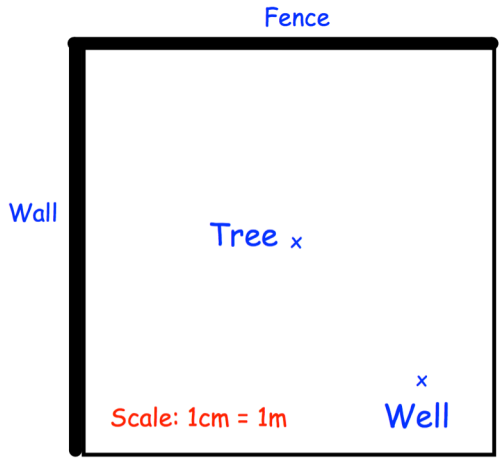
(h) A farm is equidistant from the airport and Redville **and** equidistant from the airport and the harbour.

Question 1:

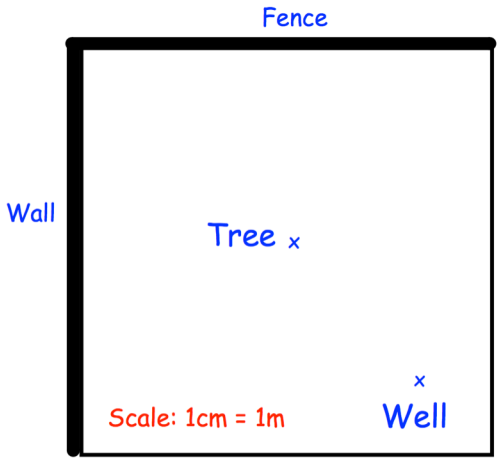
(a)



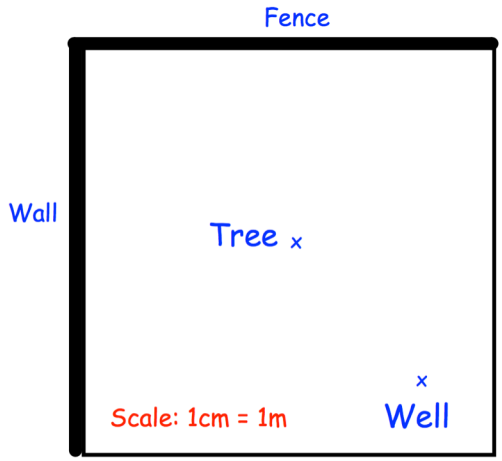
(b)



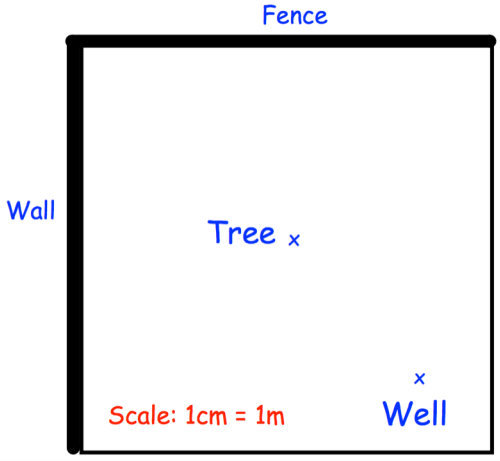
(c)



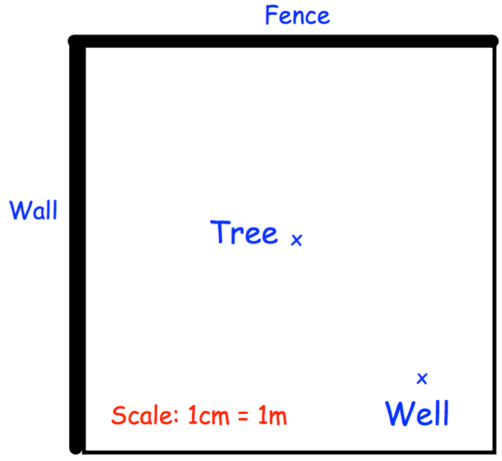
(d)



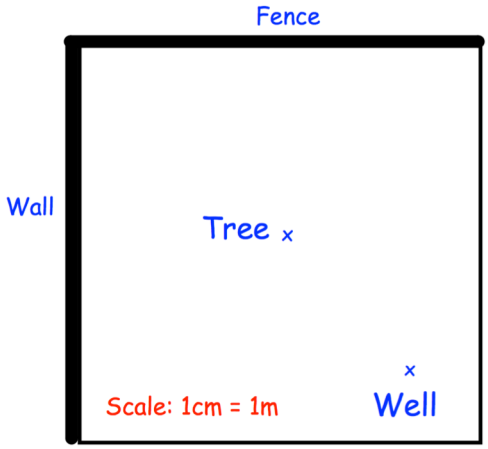
(e)



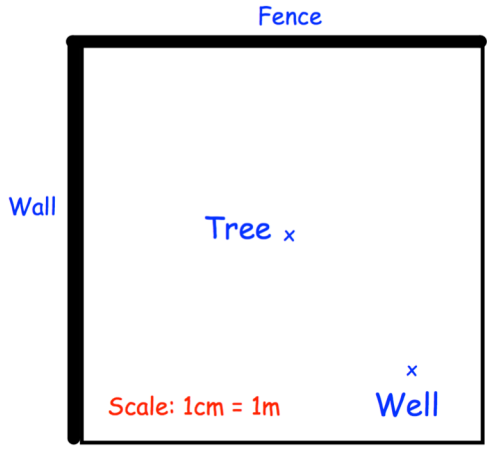
(f)



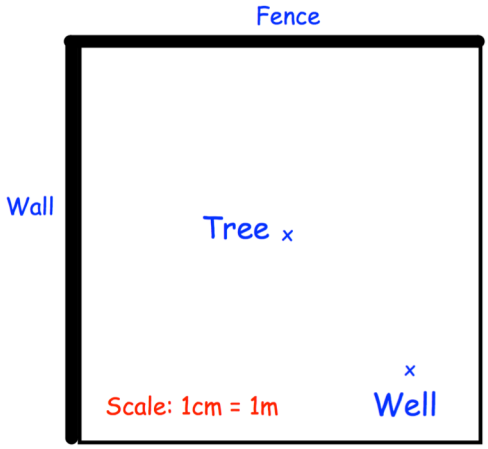
(g)



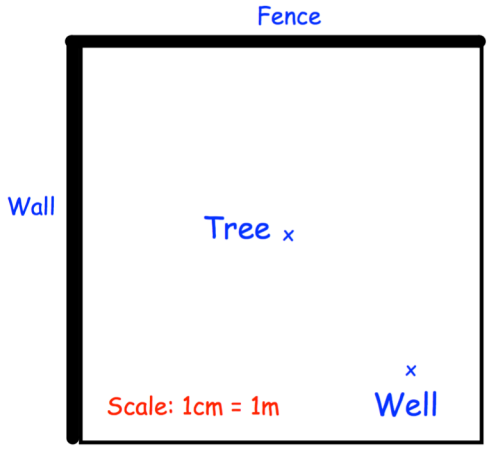
(h)



(i)

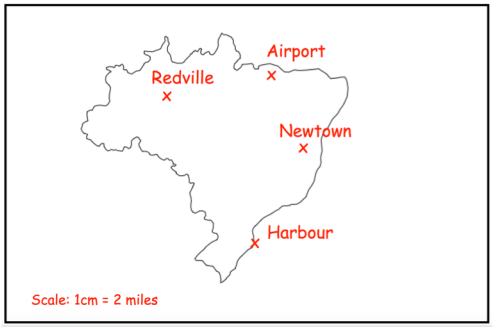


(j)

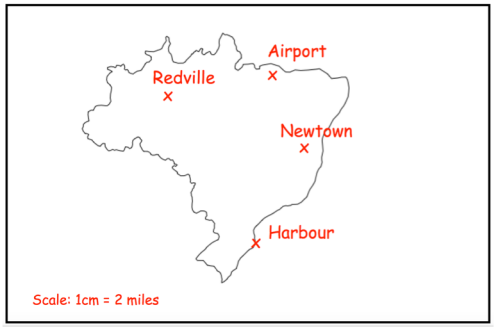


Question 2

(a)



(b)



(c)

Airport
Newtown
Harbour
Redville
Scale: 1cm = 2 miles

(d)

Airport
Newtown
Harbour
Redville
Scale: 1cm = 2 miles

(e)

Airport
Newtown
Harbour
Redville
Scale: 1cm = 2 miles

(f)

Airport
Newtown
Harbour
Redville
Scale: 1cm = 2 miles

(g)

Airport
Newtown
Harbour
Redville
Scale: 1cm = 2 miles

(h)

Airport
Newtown
Harbour
Redville
Scale: 1cm = 2 miles

Extra Notes